ANALYZING METHODS OF MITIGATING INITIALIZATION BIAS IN TRANSPORTATION SIMULATION MODELS

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ANALYZING METHODS OF MITIGATING INITIALIZATION BIAS IN TRANSPORTATION SIMULATION MODELS

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SUMMARY

All computer simulation models require some form of initialization before their outputs can be considered meaningful. Simulation models are typically initialized in a particular, often “empty” state and therefore must be “warmed-up” for an unknown amount of simulation time before reaching a “quasi-steady-state” representative of the systems’ performance. The portion of the output series that is influenced by the arbitrary initialization is referred to as the initial transient and is a widely recognized problem in simulation analysis. Although several methods exist for removing the initial transient, there are no methods that perform well in all applications.

This research evaluates the effectiveness of several techniques for reducing initialization bias from simulations using the commercial transportation simulation model VISSIM®. The three methods ultimately selected for evaluation are Welch’s Method, the Marginal Standard Error Rule (MSER) and the Volume Balancing Method currently being used by the CORSIM model. Three model instances – a single intersection, a corridor, and a large network – were created to analyze the length of the initial transient for varying scenarios, under high and low demand scenarios.

After presenting the results of each initialization method, advantages and criticisms of each are discussed as well as issues that arose during the implementation. The results for estimation of the extent of the initial transient are compared across each method and across the varying model sizes and volume levels. Based on the results of this study, Welch’s Method is recommended based on its consistency and ease of implementation.
CHAPTER 1
INTRODUCTION

Over the past several decades, computer simulation has become an increasingly vital instrument for the analysis of transportation networks. By using simulation, complex networks can be analyzed in a risk-free environment to test assumptions and preview possible outcomes to determine their potential for implementation [1]. Simulation provides an enormous amount of flexibility to manipulate conditions that could influence the operation of the network. For instance, if an impact analysis of the closure of two lanes due to an accident or construction is desired, simulation can be used to model the impact on the network without the need to physically close the two lanes. Another example would be if several proposals for the configuration of an interchange are being considered, an analyst can run a computer simulation model of each alternative to see which proposal can maximize the operational efficiency.

The ability to integrate traffic demand forecasting into simulation models can be extremely useful for transportation planning purposes. Simulations can be utilized to model the performance of the existing roadway under future demands to help determine which arterials cannot handle future capacity and need expanding. Given the myriad of ways transportation simulation can be used to critically analyze travel conditions, it is extremely important that the data processing aspect of the simulation analysis be fundamentally sound. One area requiring additional development is guidelines to govern the initialization of transportation simulation models in the determination of when it is appropriate to begin collecting statistics.
The simulation start-up problem is of significant interest and has been studied greatly in literature. When a model is initialized in a condition uncharacteristic of steady-state, bias may be introduced into determined estimators leading to inaccurate results. There are two common methods of mitigating the initialization bias problem. The most common approach is truncation, or discarding the initial data influenced by the starting conditions. The second approach is intelligent initialization, or starting the model in a state with a high probability of equilibrium. However, it is not always convenient or even practical to start the simulation in such a state [2]. More importantly, determining what equilibrium means in a transportation model can be difficult and arbitrary. For example, determining \textit{a priori} how many vehicles to queue at each light, where to place all the vehicles, and what initial speed is nearly impossible in most instances.

A possible challenge to the use of simulation models for analysis is determining if the given model reaches steady-state. For instance, some argue that transportation models never achieve stationarity because they not converge on a constant value [3]. Due to the nature of traffic signals, vehicles arrive in platoons and travel times can fluctuate substantially over the course of several minutes. Thus, as a part of this effort a definition of steady-state will also be established.

1.1 Need for Study

The need to eliminate initialization bias, also known as the start-up problem, is a widely recognized challenge with simulation analysis. This occurs because non-terminating simulations do not have predefined run lengths or initial conditions. The processes must be initialized arbitrarily, which creates bias in steady-state parameter
estimates. Although methods of removing initialization bias exist, there is currently no largely accepted method that performs suitably in all applications. Additionally, there is an overall negligence of the initial transient problem in practice [4]. Robinson (2005) stated that “the availability of commercial simulation software has placed simulation model development into the hands of non-experts by removing the need for a detailed knowledge of programming code” [5]. As a result, many simulation models are likely being improperly used.

1.2 Study Objective

The purpose of this study is to analyze the effectiveness of several techniques in eliminating initialization bias from transportation simulation models. A survey of the various methods will be discussed, and the top three methods will be compared in detail to examine their performance. The performance of these truncation methods will be tested on a simulation model using PTV-VISSIM® 5.10.

1.3 General Procedure

The general framework that will be used to analyze the initialization bias mitigation methods is outlined below:

1. Steady-state in simulation must first be defined.
2. Existing methods of removing initialization bias are surveyed.
3. Three truncation methods are selected based on popularity and effectiveness.
4. VISSIM® models are created for varying network sizes.
5. Measures of Effectiveness (MOE) for each network are determined.
6. Each truncation method will be applied to the selected MOE under non-congestion conditions.

7. The methods will be reapplied for cases when the network approaches congestion.

1.4 Study Overview

This study compares the proposed initialization bias truncation methods on three different networks. First the methodology is tested on a single intersection modeled after the 5th Street and Spring Street intersection in Atlanta, Georgia. Second, this study area is expanded to a corridor of 5th Street consisting of five signalized intersections. Finally, a large network encompassing the Georgia Tech campus and surrounding area is analyzed, including the 5th Street corridor. This large network is approximately 18 by 22 blocks and consists of 87 signalized intersections. Each network is simulated for both under-capacity and near-capacity conditions. This analysis allows for a study of the impact of network size and traffic demand on the initial transient in the transportation setting.
CHAPTER 2
LITERATURE REVIEW AND BACKGROUND

The purpose of this research is to determine when a simulation model has reached equilibrium, or steady-state. This will allow for the identification and elimination of the initial transient and the determination of unbiased (regarding model start-up) performance measures. However, before the initial transient may be identified a general definition of steady-state must be established as well as a definition of steady-state specific to transportation simulation models. For transportation simulation applications this effort will focus on microscopic simulation models.

After defining the initial transient current methods of removing the initial transient in simulation output data found by reviewing relevant literature will be introduced. The majority of this literature was selected from the Proceedings of the Winter Simulation Conference, the European Journal of Operational Research, and the Naval Research Logistics Quarterly. The methods currently being used by the simulation tools VISSIM®, CORSIM, and TransModeler are examined as well. Finally, three methods selected for implementation within this research are identified and further discussed.

2.1 Defining Steady-State

Simulations can be classified as either terminating or nonterminating. A terminating simulation has a “natural” event that specifies the duration of each run [3]. An example would be a restaurant open from 8:00 A.M. to 10:00 P.M. and observing the
number of transactions occurring within that finite time period. A non-terminating simulation has no natural event to specify the run length [3]. An example is a continuous process with no ending conditions, such as traffic flowing on a freeway. In this study the steady-state parameters of interest are estimated from non-terminating simulations. Two strategies for calculating the steady-state mean of the performance measure of interest are:

1. **Fixed sample size** – A single run of arbitrary length is conducted and a confidence interval is constructed about the sample mean.

2. **Sequential procedures** – Simulation length is sequentially increased until an “acceptable” confidence interval is achieved [6].

This study focuses on fixed sample size procedures that can be used after the simulation has been performed for a predefined amount of time, long enough to allow the model to reach a steady-state. Fixed sample size procedures are the primary considerations as much of current transportation simulation practice and tools follow fixed sample size techniques. Future research efforts will explore the use of sequential procedures to determine if a more significant change to the current state of the practice can realize significant analysis benefits.

Most transportation simulations (e.g. VISSIM® which is used in this effort) incorporate stochastic distributions (for speed, acceleration, deceleration, and various driver behavior characteristics) due to the inherently variable nature of traffic[7]. A stochastic process is “a collection of similar random variables ordered over time,” and can either be discrete or continuous-time stochastic processes [6]. As the simulation models use random variables as input, the simulation output data vary randomly over a
particular range. Parameter estimates are based on observations of the simulation process, and cannot be exactly representative of steady-state behavior, as the steady-state distribution is unknown. Characteristics of most real-world systems change over time and do not have a true steady-state distributions [3].

One must make assumptions to draw inferences about the stochastic process, in order to analyze a set of simulation output data. One example is to assume that the stochastic process is covariance-stationary. This is defined by Law and Kelton as:

$$\mu_i = \mu \quad \text{for } i = 1, 2, \ldots \text{ and } -\infty < \mu < \infty$$

$$\sigma_i^2 = \sigma^2 \quad \text{for } i = 1, 2, \ldots \text{ and } \sigma^2 < \infty$$

For covariance-stationary processes, the mean and variance are stationary over time, and the covariance between two observations depends only on their separation in the time series, not on the actual values of $i$ [6]. Furthermore, steady-state does not mean the random variables will take on the same values every time; rather they will have approximately the same distribution. The rate of convergence of the transient distribution depends on the initial conditions; however the steady-state distribution does not [6].

The steady-state average, $\mu$ is defined by Law and Kelton as:

$$\mu = \lim_{i \to \infty} E(Y_i) \quad \text{or} \quad \mu = \lim_{m \to \infty} \frac{\sum_{i=1}^{m} Y_i}{m}$$

In this study, steady-state is defined as the characteristics of the model obtained after the simulation has been running for a finite time of sufficient length such that the
output is “relatively free of the influence of initial conditions” [8]. This definition is inherently subjective as the user is responsible for choosing the run length and depends on the user’s interpretation of ‘relatively free of influence’. Determining the length of the simulation run depends on the size of the network, however, in steady state the characteristics of model should take on the same distributions compared to a model run for an extremely long time (infinite in theory).

Analysts are typically interested in several performance measures from the output data. Each separate performance measures could reach steady-state at different times, thus it is important to check each performance measure for initialization bias and use a start-up time that is adequate for all of them [9].

2.2 Steady-State in Transportation

Transportation simulation is similar to a queuing system, but varies because: 1) in many instances faster vehicles can overtake slower vehicles without having to wait behind, 2) vehicles can change lanes easily as opposed to often fixed queues in servers, 3) capacity is a continuous constraint over the entire roadway, not just a point constraint, 4) congestion can occur unexpectedly, and 5) traffic demands indicate strong time-series patterns rather than random distributions [1].

There are several performance measures that can be used to determine when a transportation simulation model is in steady-state. The measures of effectiveness selected for this experiment are the number of vehicles in the network and the average travel times across the network. Calculating the number of vehicles in the network for a given time interval allows for the determination of when the entering and exiting volumes are
balanced, a common intuitive measure of when the system is “full”. Travel times record the amount of time it takes a vehicle to traverse the model which is made up of the free flow time plus the delay encountered by the vehicle. Travel time (along with delay as a standalone component) is a common utilized performance metric. If the model does not reach a steady-state, it is expected that the number of vehicles in the network and the travel times would constantly increase.

It is noted that other performance metrics could be utilized to test for steady state, e.g., queue length, average link speed, etc. However, in this effort the number of vehicles in the network and travel time are utilized due to their ability to aid in the intuitive understanding of model performance and their common use in practice. Future efforts however should be undertaken to consider the potential benefits of alternative measures or combinations of measures.

2.3 Methods of Truncating the Initial Transient

A survey of methods used to delete the data affected by the initial transient of discrete event stochastic simulation models is discussed. These methods of initializing simulation models seek to provide more accurate results for the steady-state estimates of the mean. The methods can be grouped into the following categories as described by Robinson (2007): graphical, heuristic, statistical, initialization bias testing, and hybrid methods [10].
2.3.1 Graphical Methods

The most common methods to identify the initial transient are graphical procedures. Graphical procedures consist of a visual inspection of the time series to determine the extent of the initial transient. A major advantage is the simplicity of these methods and their reliance on few assumptions. These methods are typically highly subjective as the truncation points could vary based on the judgment or experience of the analyst.

2.3.1.1 Fishman’s Method (Column Averages)

Two types of error present in discrete event simulation are sampling error (caused by random input) and systematic error (due to the initial transient) [8]. To detect the systematic error, multiple independent replications are needed to reduce the sampling error. Fishman proposed to plot the sequence of column averages to visually determine a suitable warm-up [11]. To calculate the column average, independent replications of a predefined length are lined up in rows and the average value is determined for each observation. In the Figure below, $Y_{ij}$ represents the $j$th observation of the $i$th replication.

<table>
<thead>
<tr>
<th>Replication</th>
<th>$Y_{11}$, $Y_{12}$, $Y_{13}$, $Y_{14}$, ..., $Y_{1j}$</th>
<th>$Y_{21}$, $Y_{22}$, $Y_{23}$, $Y_{24}$, ..., $Y_{2j}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$n$</td>
<td>$Y_{n1}$, $Y_{n2}$, $Y_{n3}$, $Y_{n4}$, ..., $Y_{nj}$</td>
<td></td>
</tr>
</tbody>
</table>

| Column Averages | $\bar{Y}_1$, $\bar{Y}_2$, $\bar{Y}_3$, $\bar{Y}_4$, ..., $\bar{Y}_j$ |

Figure 1. Calculation of Column Averages, following Law (2007)
Fishman’s method requires multiple replications in parallel and an experienced user to determine the warm-up from the graph. The steps for Fishman’s method are as follows:

1. Choose the run length $t$ and number of replications $n$.
2. Compute the average values over every replication at each time step.
3. Plot the column, and if the graph “fails to reveal a suitable warm-up,” iteratively increase the run length and the number of replications [8].

2.3.1.2 Welch’s Method: Moving Averages

Welch’s method is a simple and general technique for determining when a model reaches steady-state that can be considered an extension of Fishman’s Method [6, 11]. Welch’s Method consists of plotting a sliding window of the sequence of column averages in an attempt to reduce the effects of the systematic error. It requires multiple replications with the goal of determining the smallest window size that best smoothes the plot of the moving averages, allowing the sequence to converge to a constant value where the truncation point can be visually identified. Welch (1983) stated that the window should be “long enough to remove short term fluctuations but not so long as to distort the long term trend” [12].

A major concern in applying Welch’s procedure in practice is the large number of replications required if the process is highly variable. Another disadvantage is that smoothing the data can lead to inaccurate results. Finally, the determination of the “smoothness” of the plot and the convergence point is based on the user’s subjective judgment.
2.3.2 **Heuristic Methods**

These methods provide definitive rules or formulas to determine the length of the warm-up period. The advantages of these methods are lack of user specific subjectivity, ease of implementation, and the few assumptions needed. However, if the output series is not visually inspected, important patterns could be overlooked.

2.3.2.1 **Marginal Standard Error Rule (MSER)**

First proposed by White in 1997 as the Marginal Confidence Rule, the goal of this method is to find the truncation point that best “balances the tradeoff between improved accuracy (elimination of bias) and decreased precision (reduction in the sample size)” [13]. A key assumption of the MSER is the observations in the second half of the simulation are closer in value to the true steady-state mean. White proposes to “select a truncation point that minimizes the width of the marginal confidence interval about the truncated sample mean” [14]. The expression for the optimal truncation point, $d_j$ is shown below:

$$d_j^* = \arg \min_{n>d(j)\geq 0} \left[ \frac{1}{(n(j) - d(j))^2} \sum_{i=d+1}^{n} \left( Y_i(j) - \bar{Y}_{n,d}(j) \right)^2 \right]$$

MSER applies to the raw output series, $Y_i(j)$ and the truncation point, $d_j$ is selected at the minimum value of this function. MSER tests to see if an observation prior to the proposed truncation point is representative of the sequence observed after this point, and if including the prior observations would increase the marginal confidence in the estimator [13].

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2.3.2.2 Marginal Standard Error Rule (MSER-5)

A slight modification to MSER, this method examines a series of batch averages and uses the same formula to compute the optimal truncation point. White Jr. et al. (2000) determined the performance of MSER can be improved by using batch means, specifically a batch size of five [14]. The process is calculated using nonoverlapping batches; the rule evaluates the removal of leading batches and calculates the width of the confidence interval on the remaining data set. After the optimal truncation point has been selected, the resulting truncated batch means are assumed to have minimal MSE and be free of initialization bias [15].

This method has been shown to produce desirable results by minimizing the width of the confidence interval, however, one critical problem found with the MSER-5 method is the technique can be very sensitive to outliers, which can result in poor performance. In a study by Sandikçi and Sabuncuoğlu using MSER-5, the output data contained 8 extreme data points and the suggested truncation point was at 4800 observations. However, if the outliers were removed the truncation point changed to 340 observations [4].

2.3.2.3 Conway’s Rule

Conway (1963) proposed to “truncate a series of measurements until the first of the series is neither the maximum nor the minimum of the remaining set” [16]. This method would not be suitable for transportation models due to the variability in the simulation process. Output data from transportation models tends to have cyclic patterns
due to the operation of signal controllers, which would often result in assuming the model has reached steady-state too early.

2.3.2.4 Crossing of the Means Rule

Proposed in by Fishman (1973), this method requires the analyst to “compute the running cumulative mean as data are generated. Count the number of crossings of the mean, looking backwards to the beginning. If the number of crossings reaches a pre-specified value,” the resulting value is the proposed truncation point [17]. While the method removes subjectivity from its application in a particular instance the method itself remains highly subjective. It requires the user to predefine the number of crossings that will be used, leading to arbitrary truncation points. For instance, in a study performed by Gafarian et al. (1978), a value of three was used [18], however, little justification exists for applying this results directly to the transportation application.

2.3.2.5 Replicated Batch Means

This method attempts to combine independent replications (IR) and batch means (BM) to estimate steady state characteristics. Using the IR method, $r$ independent runs are performed and the sample average is computed for each run. Conversely, the BM method consists of performing a single, long run and dividing the output into $b$ continuous batches [19]. There is a tradeoff between using a single, long run and making many replications:

- Using IR, the replications are independent of each other; however, each trial is influenced by initialization bias created from starting up the simulation run.
- With BM, initialization only occurs in the first batch, but adjacent batches are usually correlated to each other [19].

Replicated batch means (RBM) combines the two methods in an attempt to benefit from each of the method’s advantages. Argon et al. (2006) propose conducting a few independent replications, each including the same number of batches[20]. Numerical results from the 2006 study produced confidence interval estimates that were similar to substantially better than results obtained by BM [19].

### 2.3.3 Statistical Methods

These methods rely on the statistics principles to determine the warm-up period. Disadvantages tend to include the complexity of these procedures, constraining assumptions, and increased computing time.

#### 2.3.3.1 Randomization Test

The Randomization test sets a null hypothesis that there is no initialization bias. The sample is divided into \( b \) batches and the grand mean of the first batch is compared to the grand mean of the remaining batches. If the difference is significant, the null hypothesis is rejected, the batches are regrouped, and the second batch is added to the first group. The grand means of the first two batches are compared to the remaining \( b-2 \) batches to see if they are significantly different. This process is repeated until the hypothesis is accepted and the transient is detected. The second group of batches represents the steady-state simulation output [17, 21]. As with the previous methods the
users must still make a number of subjective assumptions, for instance, the batch size can significantly influence results.

2.3.3.2 Welch’s Regression-Based Method

The goal of this statistical procedure is identify an appropriate truncation point and run length by fitting a straight regression line to the second half of the data. After the output is grouped into batches, a straight line is fit to the batch means of the second half of the data using generalized least squares (GLS) [22]. If the slope of the line is “significantly different from zero,” the run length must be increased. Once enough data is collected, a reverse pass through the sequence is performed and the simulation is considered to be in steady state as long as the fitted line continues to have a zero slope [22]. However, Law and Kelton (2000) noted several theoretical limitations of this approach, such as the fundamental assumption that the process converges to $\mu$ monotonically, and declined to test it further [3]. Other criticisms noted by Hoad et al. (2008) are the high number of parameters needed (nine), the procedure is computationally intensive and can be complex to execute [23].

2.3.3.3 N-Skart

The purpose of the N-Skart method is to create a confidence interval (CI) for the mean with the desired coverage probability $(1 - \alpha)$ specified by the user. This is achieved by employing von Neumann’s Randomness test to spaced batch means to determine the point after which the batches are independent and uninfluenced by the initial conditions [15]. N-Skart makes modifications to the non-spaced batch means’ CI to correct the
underlying skewness and autocorrelation. “The skewness adjustment is based on the Cornish-Fisher expansion for the t-statistic, and the autocorrelation adjustment is based on a first-order autoregressive approximation to the batch means autocorrelation function” [15].

When compared to the MSER-5 method, N-Skart showed significantly less bias and variance. However, N-Skart is significantly more complicated and more efficient versions are needed to reduce processing time [15].

2.3.3.4 Automated Simulation Analysis Procedure (ASAP)

ASAP is an algorithm for simulation output analysis based on nonoverlapping batch means. For ASAP3 (a refinement of ASAP and ASAP2), the batch size is increased until the batch means pass the Shapiro-Wilk test for multivariate normality, ASAP3 fits a first-order autoregressive time series model to the batch means [24]. Next, ASAP3 delivers a correlation-adjusted confidence interval (CI). In the case study reported in Steiger et al. (2004), the simulation is initially divided into 256 batches (with 400 long run independent replications being performed). The first 4 batches are ignored and every other group of 4 consecutive batches are selected and tested for multivariate normality. If failed, the batch size is increased by a factor of $\sqrt{2}$. Correlation between adjacent batches is tested to ensure that it does not exceed 0.8. The confidence intervals are then constructed and check to see if they meet the precision requirements [24].

This method requires a large amount of replications, and an analyst with a great amount of expertise to perform. ASAP also requires a precision requirement and at this time, it would not be suitable for transportation applications.
2.3.4 Initialization Bias Tests

The goal of initialization bias testing is to determine if bias is present in the data due to the initial transient. The majority of these methods build upon the work of Schruben (1982) [10]. The general procedure is to divide the output series into $b$ batches of equal length and subsequently group into two sets: $b'$ and $b-b'$[14]. The estimates of the mean and variance are used to compute a test statistic which is compared to an appropriate F distribution [14]. Hypothesis testing is performed with the null hypothesis that no initialization bias exists. These procedures can also be used in union with previously described methods to determine if initialization bias has been successfully removed.

2.3.5 Hybrid Methods

Hybrid methods are a combination of two methods, usually initialization bias testing and either a graphical or heuristic method. These methods are typically complex and can require large amounts of data [10].

2.3.5.1 Statistical Process Control

The statistical process control (SPC) method can be classified as a hybrid; a combination of a graphical and heuristic methods. In this approach a simulation model is considered “out of control” while in its transient phase and once it has reached steady-state, “in-control”. The goal of the SPC method is to determine when a model is “in control” and thus when the model is no longer influenced by its initial state [10].

The 4 steps for the SPC method are:
1. Perform experiment and collect data.

2. Test the second half of the data to check that it is distributed normally and not correlated. The SPC approach must meet these two conditions, therefore:
   
   - As simulation output is typically a correlated time series batch means represent one method to account for this autocorrelation. However, one issue with batch means is determining the batch size. This procedure requires that the batch size be doubled until the null hypothesis (that there is no correlation between batches) is accepted. The minimum batch size for which there is no correlation is sought.
   
   - The data must pass the test for normality at each selected batch size. Different methods of testing for normality include:
     
     o Chi-square test
     
     o Kolmogorov-Smirnov test
     
     o Anderson-Darling test
   
   - If the number of batches is less than 20, a longer simulation run is needed.

3. Construct a control chart.
   
   - It is assumed the process is stable during the second half of the data. Estimates for the population mean and standard deviation are taken from this portion of the time series.
   
   - Three sets of control limits are calculated accordingly:
     
     $CL = \hat{\mu} \pm z\sigma / \sqrt{n}$ for $z = 1, 2, 3$

4. Determine the initial transient.
• To plot the control chart, the mean, three sets of control limits, and the time-series output are graphed.

• Rules for determining when the series is “in control” and “out of control” are given that are based on where the data falls within the three sets of control limits [10].

Montgomery and Runger (1994) established the following rules to determine when the process is “out of control”:

• A point plots outside a 3-sigma control limit.

• Two out of three consecutive points plot outside a 2-sigma control limit.

• Four out of five consecutive points plot outside a 1-sigma control limit.

• Eight consecutive points plot on one side of the mean [10].

Bias, coverage, and the expected half-length of the confidence interval are the performance measures are evaluated by Robinson. Using the SPC method easily increased the accuracy of the steady-state parameters compared to not deleting any initial data [10]. However, it is important to note that this method (as well several others discussed) assumes the model is in steady-state for the second half of the simulation run. If the model fails to reach a steady state this method will likely not identify this condition, potentially erroneously identifying the end of the initial transient.

2.4 Methods currently used by simulation models

A survey of three traffic simulation models was conducted. Technical support for two of these models was contacted to see how they approached the warm-up problem in their respective software, and if the simulation models had built-in methods of
initializing the network. Two of the three models have a built-in function to determine when the network has reached “equilibrium”.

2.4.1 PTV Vision – VISSIM®

Correspondence was made with support at PTV-VISSIM® June 7, 2010 to inquire how they mitigate the initialization bias problem. The response was the length of the warm-up period is always dependent on the size and characteristics of the network, and that this seeding period should be at least as long as the travel time of the longest possible path through the network. Further correspondence was made (August 2, 2010) to ask if PTV was planning on implementing a built-in method of determining equilibrium in future releases, similar to some of its competitors. To their knowledge, no such procedure is in progress.

2.4.2 McTrans – CORSIM’s Volume Balancing

No contact was made with CORSIM, however their built-in equilibrium procedures were studied. The Federal Highway Administration created a set of guidelines for applying simulation analysis entitled “Traffic Analysis Toolbox” with Volume IV containing Guidelines for Applying CORSIM [25]. Before it is acceptable to start accumulating statistics, CORSIM first determines when the model has reached equilibrium. To do this, there is a built-in heuristic method that compares the number of vehicles in the network at consecutive time intervals. It determines equilibrium has been reached “if the difference between the current interval and the previous interval is less than eight percent and the difference between the previous interval and the one before it
was less than 12 percent… If those conditions have not been met, but the difference between the current interval and the previous interval is less than six percent” the model has reached equilibrium [25]. The user has the option to enter a maximum initialization time and once it has been reached, the model can either collect data if it is in equilibrium, or abort if it is not. It can be helpful to force the maximum initialization time if the model appears to incorrectly determine it is in equilibrium.

There are some disadvantages of using this method to determine equilibrium. First, if a small time interval is chosen (such as one second), this method could determine equilibrium has began prematurely because the volumes would not be expect to change significantly in such a short period. Similarly, a large model with high volumes could terminate the initialization period too soon because the percentage change in volume would become less sensitive [25].

2.4.3 Caliper Corporation – TransModeler®

Contact was made with a transportation engineer at Caliper Corporation August 10, 2010 in inquire about the equilibrium capabilities of TransModeler®. The response was that TransModeler® does implement a method of comparing the number of vehicles in the network similar to CORSIM, however it is optional. Caliper continually surveys research literature for other possible methods.

2.5 Selection of Methods

Hoad et al. (2008) performed a seminal study on the existing methods of estimating the length of the warm-up period in hopes of producing an automated
procedure to be included in simulation software [23]. The authors conducted a comprehensive review of literature and found 42 methods for detecting the extent of the warm-up. These methods were evaluated and graded based on the following criteria: accuracy and robustness of method, simplicity of the model, ease of potential automation, generality, number of parameters required, and computing time [23]. The list was narrowed down to six methods for further evaluation, excluding graphical methods due to their need for human intervention. Of the six methods, MSER-5 substantially outperformed the rest while the other methods either severely underestimated the truncation point or required an extremely large number of replications.

The criteria that were used to determine the selected methods for this study are their ability to be implemented, their effectiveness, and their popularity. While the graphical methods were not included in the study performed by Hoad et al. (2008) because of the difficulty automating the procedure [23] this experiment will evaluate the graphical procedure, Welch’s Method, based on its simplicity and overwhelming popularity. MSER-5 will also be implemented in this study due to its effectiveness, frequent use in the industry, and ease of implementation. A third method that will be examined is the volume balancing method currently used by CORSIM and TransModeler®.
CHAPTER 3

METHODOLOGY

The truncation methods discussed earlier were separated into the following categories: graphical, heuristic, statistical and initialization bias testing. Of the graphical procedures proposed, Welch’s Method is widely used and perhaps the most referenced method in literature. The steps needed to implement this procedure are detailed in this chapter. For the heuristic approaches, it appears MSER-5 is the most effective method and would be most applicable for this experiment. The formula for the MSER heuristic is listed in this chapter, as well as issues with implementation. The third method selected is the volume balancing procedure used by CORSIM (and similarly by TransModeler®), which a simple mathematical heuristic. This is selected as it is the only method identified as commonly used in transportation microscopic simulation applications. Each methodology will first be performed on the number of vehicles in the network to determine steady-state. Next, the network travel times will be examined and each method re-applied.

3.1 Welch’s Method

The steps and equations for calculating Welch’s Method of moving averages for a window size, \( w \) are listed below [3, 6]:

1. A number of replications \( n \geq 5 \) is performed, each of length \( m \), where \( m \) is much larger than anticipated truncation point. The observations are averaged over all replications at each time-step to create the average process, \( \bar{Y} \).
3. The moving averages, $\bar{Y}(w)$ are plotted for several values of widow size, $w$. An initial value for $w$ is 1, and then increased in increments of 1, where $w \leq m/4$.

$$\bar{Y}_i(w) = \begin{cases} 
    \frac{1}{2w + 1} \sum_{s=-w}^{w} \bar{Y}_{i+s} & \text{if } i = w + 1, \ldots, m - w \\
    \frac{1}{2i - 1} \sum_{s=-(i-1)}^{i-1} \bar{Y}_{i+s} & \text{if } i = 1, \ldots, w 
\end{cases}$$

As shown above, a window size $w$ consists of the average of $(2w + 1)$ observations. The smallest value of $w$ for which the plots are “reasonable smooth” is selected.

4. If no value of $w$ is satisfactory, the number of replications is increased.

5. The truncation point is selected visually from the moving averages plot [3, 6].

Welch proposes starting with $n = 5$ or 10 replications, based on computing cost and time. For this experiment, we started with 10 replications and increased the number of replications if a sufficient window size could not be chosen. Based on the expected truncation value, a simulation length of five hours was selected. This run length should be more than sufficient for all transportation models tested to reach steady state well before the halfway point in the model. To implement Welch’s Method an Excel™ spreadsheet was created to generate plots of incrementally increasing window sizes. The data output was averaged over a defined number of replications (initially 10) using a separate script. In this instance the data output is a snapshot of the number of vehicles in
the network recorded every five seconds. These plots are visually inspected and if the moving averages do not sufficiently converge to a constant value, more replications are performed. Once the desired number of replications and window size are selected and it is determined that the moving averages are reasonably smooth for the five hour period, the initial portion of the plot is enlarged to examine the warm-up more closely.

An example graphical output for Welch’s Method is shown in Figure 2 below. In this example the window size and the number of replications were both increased until the plots became sufficiently smooth, resulting in a window size of 100 time steps with 40 replications as the final parameters for truncation point identification. In Chapter 4, a complete discussion on the selection of the window size and number of replication is provided.

![Graphical output for Welch’s Method](image)

**Figure 2.** Welch’s Method for 5th Street Model, window size 100, five hour run
As previously stated, to determine the point where the model reaches steady-state, the initial portion of the above moving averages plot is enlarged. A small time period is chosen that exceeds the anticipated truncation point and allows the analyst to visually detect the point at which the plot becomes smooth. A visual aid is also added to the plot to help identify when the sequence reaches the point where the plot becomes smooth. A horizontal line is added that is equal to the average of Welch’s values in the second half of the time series. This removes some of the subjectivity of visually detecting when the plots reach steady-state. Figure 3 below shows the inspection of the warm-up, plotted for the first 1200 seconds of the data shown in Figure 2. In this example, the truncation point was determined to be 600 seconds.

Figure 3. Welch’s Method Plot for Identification of Warm-up period
3.1.1 Selecting Window Size

Law and Kelton noted that “choosing $w$ is like choosing the interval width $\Delta b$ for a histogram” [6]. If $w$ is too small the plots will appear ragged, and choosing a window size too large could over-aggregate the data. Sturges’s rule is proposed to choose the interval width $\Delta b$ for a histogram as follows:

$$k = \lfloor 1 + \log_2 n \rfloor = \lfloor 1 + 3.322 \log_{10} n \rfloor$$

Using this formula for our case of 3600 observations would result in value of 12.8 for the interval width. However, Law and Kelton do not believe such rules are useful and recommend trying several different values and choosing the smallest value that best smoothes the plot [6]. In this study, it was seen that the window size needed to be sufficiently large to smooth out the cyclic trends due to the signalized intersections timing plans.

3.1.2 Travel Times using Welch’s Method

As stated previously, in addition to performing Welch’s Method on the number of vehicles in the network, Welch’s Method is applied to network travel times. While the same method is being applied to these output values, there are some small differences in the method application to the data. As noted the number of vehicles in the network is a snapshot every five seconds during the simulation. However, travel time is measured along a pre-specified path through the network. Vehicles complete their traversal of this path randomly, based on their arrival into the network and in-network experience. Thus,
travel time measures at specific time intervals are not necessarily meaningful. It is more
appropriate to consider the travel time measurements as individual observations. It is
noted that as an implementation issue in the specific data collection technique utilized
that multiple vehicles existing the network during the same five second interval will be
assigned the same travel time.

3.2 Marginal Standard Error Rule (MSER-5)

The Marginal Standard Error Rule is be implemented in this as it has been found
to an effective heuristic by multiple studies [4, 13, 14, 23, 26]. The expression for the
optimal truncation point is given in White Jr. (1997) as:

\[
d_j^* = \arg\min_{n>d(j)\geq0} \left[ \frac{1}{(n(j) - d(j))^2} \sum_{i=d+1}^{n} \left( Y_i(j) - \bar{Y}_{n,d}(j) \right)^2 \right]
\]

\[
d_j = \text{Truncation point at proposed time (} j \text{)}
\]

\[
n = \text{Total number of batches}
\]

\[
Y_i = \text{Value at proposed truncation time (} j \text{)}
\]

\[
\bar{Y}_{n,d} = \text{The average value of remaining sequence (from} n \text{ to} d \text{)}
\]

A major assumption of MSER is that the data on the second half of the sequence
is more characteristic of steady-state conditions. The width of the confidence interval
about the truncated sample mean is minimized to balance the tradeoff between improved
accuracy and decreased precision. For this rule to be successful, the simulation length
must be long enough such that a false steady-state is not observed.
3.2.1 Batch Size Selection

The first step to analyzing the MSER is to batch the data. The purpose being that batching the observations “ensure the monotonic behavior of the decrease in confidence interval width” [26]. It is important to recall that in the current application performance statistics were collected every five seconds. Each snapshot at the end of five seconds is considered a single observation. Using this original data in the application of the MSER method will be referred to as MSER-1 because no batching is undertaken. Next, the MSER is performed for \( n = 5 \) batches, which covers 25 simulation seconds (i.e. five, 5-second batches). Additional results for the MSER-n will analyzed for batch sizes of 12 and 22, corresponding to 60 and 110 simulation seconds. MSER-22 was selected to allow for a test of the method using a batch size equal to the cycle length of the major network intersections. MSER-12 was selected to allow for a testing of the method for an equivalent simulation time period (i.e. 60 second) as utilized by default in the CORSIM Volume Balancing procedure.

3.2.2 Using MSER on Multiple Replications

As with Welch’s Method multiple replications helps to ensure accuracy in the identification of the end of the initialization transient. However, the approach for using multiple replications is different for the MSER. White Jr. (1997) noted that the Marginal Confidence Rule (later named MSER) was not intended to be used over the average of many replications. White stated “this rule applies to individuated output sequences and has the inherent advantage of specifying the best truncation point for each such sequence, rather than a single truncation point, which is best only on average across a very large
number of replications” [13]. Therefore, in this effort MSER is performed on each individual replication, with 100 replications being performed. The statistics that will be collected for the MSER truncation points are the maximum, average, and 95th percentile. These results are shown in Chapter 4.

3.3 Volume Balancing (CORSIM)

This method could be considered a heuristic approach. In the method the percent difference in vehicles in the network between consecutive intervals is analyzed. In CORSIM if two consecutive percent differences are 12% or less followed by 8% or less the model is considered to be in steady state. The calculations for this method are straightforward; however the analyst is free to choose the interval size. The data for this experiment was collected in five second increments to allow for flexible post processing. This procedure will be performed on varying interval sizes as mentioned before, including a multiple of the cycle length. CORSIM uses an interval of 60 seconds to determine equilibrium. It is noted that no literature was found regarding the background or development of this method.

3.3.1 Multiple Replications

Similar to the MSER, averaging multiple replications would only smooth the initial transient truncation point to an average value, whereas we are interested in the maximum amount of time needed to initialize individual runs of the model. Thus, this procedure will be performed on each individual replication and the maximum, average, and 95th percentile truncation point will be collected.
3.4 VISSIM® Model Characteristics

First, the characteristics of the VISSIM® simulation model are discussed. The locations of the selected models are shown in detail and the performance measures used to evaluate the model are discussed. The experiment design is explained to clarify which models and conditions will be tested on Welch’s Method, MSER, and the Volume Balancing procedure.

3.4.1 VISSIM® Overview

VISSIM® is a microscopic, behavior based traffic simulation model which uses continuous time-step advancements to move through simulation time [7]. Networks are created using links and connectors, where links represent sections of the road and connections allow the vehicles to move between these links. Signal controllers, stop signs, reduced speed areas, priority rules and most importantly, the car following model and lane changing logic control the movement of vehicles. The accuracy of the model depends highly on the quality of the vehicle modeling and the ability of the user to model the respect network (e.g. intersection, arterial, freeway, etc.) geometry. VISSIM® uses a complex psycho-physical driver behavior model developed by Wiedemann (1974) [7]. This model is based on individual drivers’ perception thresholds of slower moving vehicles.

As VISSIM® creates a vehicle to be input into the network, specific driver behavior characteristics are assigned randomly to each vehicle. Each driver in turn, reacts based on the technical capabilities of his vehicle. Characteristics of each driver-vehicle-unit can be classified into the following categories:
1. Technical specifications of the vehicle: (length, maximum speed, potential acceleration, actual position in the network, actual speed and acceleration).

2. Behavior of driver-vehicle-unit: (sensitivity thresholds and ability to estimate, aggressiveness, memory of driver, acceleration based on current speed and driver’s desired speed).

3. Interdependence of driver-vehicle-units: (reference to leading and following vehicles on own and adjacent travel lanes, reference to current link and next intersection, reference to next traffic signal) [7].

3.4.2 Design of Experiment

This experiment compares the performance of initialization bias truncation procedures in transportation microscopic simulations, utilizing VISSIM® simulation models as the example applications. Three model sizes were developed for this study, covering an increasing geographic area. A single signalized intersection was first analyzed to determine the results for a small model. Next, a corridor consisting of the single intersection and four additional signalized intersections is tested. The corridor model is referred to as the medium network size in this study. Lastly, a large network containing the previously analyzed corridor is studied to determine the extent of the initial transient for varying model sizes. This would ensure that the geometry and signal timing of the small and medium segments are consistent across the experiment.

For each model the initial experiments set the input volume at a medium demand level, that is, non-congested traffic although reasonable demand. The actual volumes were set based on conducting several iterations of the model and the researchers’
judgment of reasonable, uncongested flow. These scenarios allow for an analysis to test the initialization bias truncation procedures with the confounding influence of congestion. Next, the models’ input volumes are increased to the represent the peak volume of the model operating just below capacity. Finally, each model will be loaded over capacity to determine how each method handles the case where equilibrium is not achieved.

3.4.3 5th Street and Spring Street Intersection

The area for this study is in Atlanta in close proximity to the Georgia Institute of Technology (Georgia Tech) campus. The single intersection to be studied is at 5th Street and Spring Street. Spring Street is a one-way major urban arterial with four lanes, while 5th Street is an urban local street with two lanes (one lane each direction). Figure 4 on the following page displays the VISSIM® representation of the intersection.

Figure 4. 5th Street and Spring Street Intersection

(Figure Credit: VISSIM® with Google Earth [27] overlay)
3.4.4 5th Street Corridor

The 5th Street corridor (also known as Ferst Drive adjacent to the Georgia Tech campus) spans from Atlantic Drive on the west, to West Peachtree Street to the east. The model consists of a mix of four-lane major arterials with high volumes (including the one-way pair of Spring Street and West Peachtree Street) and various two-lane local roads with a relatively small amount of traffic primarily moving to and from the Georgia Tech campus. Four travel time segments for this network were defined for this network, two eastbound and two westbound. Figure 5 on the following page shows the 5th Street corridor in VISSIM®.

![Figure 5. 5th Street Corridor](image)

(Figure Credit: VISSIM® with Google Earth [27] overlay)
3.4.5 Large Georgia Tech Network

The VISSIM® model of the Georgia Tech campus and surrounding area in Atlanta, Georgia was developed by a graduate research student at Georgia Tech, Kate D’Ambrosio. The network is bounded in each direction by the following streets:

- South: North Avenue
- North: 17th Street
- East: Peachtree Street
- West: Marietta Street/ Howell Mill Road

Existing geometry was extracted by overlaying a series of scaled aerial photographs to determine the number of lanes at each intersection and the spacing between them. The signal timings for the 5th Street corridor were obtained from the City of Atlanta to match the existing conditions. More detailed information on the development of the VISSIM® model is included in the Appendix. Figure 6 shows the VISSIM® model of the large Georgia Tech network.
3.5 Performance Measures

The performance measures chosen for this case study are number of vehicles in the network and the network travel time. The number of vehicles in the network is recorded every five seconds and is calculated as the instantaneous value at the end of each five second interval. Travel time segments have been set up to record the time it takes vehicles to pass entirely through the system for specified routes. For these routes, probe vehicles have been inserted in the model to ensure a sufficient number of vehicles complete the travel time segment and use the desired path. Figure 7 and Figure 8 below
show the location of the vehicle inputs and travel time segments for the single intersection and corridor model. Figure 9 shows the location of the travel time segment for the large Georgia Tech model.

Figure 7. Location of Performance Measures for Single Intersection Model
Figure 8. Location of Performance Measures for 5th Street Corridor Model

Vehicle Inputs
V1 = EB 5th Street
V2 = SB Dalnev Street
V3 = WB State Street
V4 = NB State Street
V5 = Exiting Klaus Parking Deck
V6 = NB Fowler Street
V7 = SB Fowler Street
V8 = SB Techwood Drive
V9 = NB Techwood Drive
V10 = SB Spring Street
V11 = NB W. Peachtree Street
V12 = WB 5th Street

Travel Time Segment
B to A = WB 5th from Spring Street

Figure 9. Location of Performance Measures for Large Model

Travel Time Segment
A to B = Eastbound
10th Street to Spring Street
3.6 VISSIM® Limitations

One major limitation of this research is the given simulation model does not include pedestrians. Pedestrians can have a significant impact on the operation of signalized intersections, especially near a college campus. Additionally, bicycles were not introduced into the model. The capabilities of VISSIM® to integrate pedestrians and bicycles were not explored, but should be considered in future research.

Another issue is the accuracy of the VISSIM® model with respect to routing decisions, signal timing, and traffic volumes. The calibration process is an important aspect of simulation analysis to ensure the integrity of the results. For this effort the models were reviewed only for reasonable operations (that is, vehicle behavior and performance that was reasonable for the given network size), not necessarily calibrated to match field conditions for the given locations. These models have generic traffic demands and signal timings, although where possible known field timings were utilized. Thus, the simulations are not applicable to an operational analysis of actual conditions in the modeled areas. However, the intent of this effort is a study of initial transient, which may be accomplished using the given models.

One concern encountered in VISSIM® is whether or not vehicles queued off network or vehicles disappearing were counted in the number of vehicles in the network. Several tests were performed to determine how VISSIM® counts the number of vehicles in the network. A simple model was created where the demand greatly exceeded the capacity and it was found that the vehicle count only includes the vehicles that have entered the network, and not those queued off the network. Additional tests were
performed to see if vehicles being removed from the model are included in the vehicles in the network count; which they were not.

There are two main reasons vehicles would be removed from the network in our study. The first reason is VISSIM® by default removes stalled vehicles that are unable to make a lane change after 60 seconds to avoid unrealistic backups [7]. The second reason is that once a vehicle has been specified a certain path on a routing decision, if that vehicle is unable to change to a lane where it can make that turn, it will continue on through the intersection searching for its specified path. Once it reaches the end of the link without finding that path it is removed from the network. While this would present an issue in measuring performance characteristics of the model, the occurrences of this issue was minimal and is comparable to vehicles exiting the network into a parking lot.
The results for Welch’s Method, MSER, and the Volume Balancing Method are presented in this chapter. The sensitivity of each method’s parameters are tested and discussed. The estimated truncation point will be given for the small, medium, and large models, as well as a change from low volume to high volume.

4.1 Welch’s Method

For Welch’s Method, the procedures for selecting the window size and number of replications are first discussed. Next, the sensitivity to choosing different window sizes and number of replications is analyzed.

4.1.1 Selection of Window Size

To perform Welch’s Method, the window size \( w = 1 \) is initially evaluated and incrementally increased until the plots become smooth. Increasing the window size will smooth the plots of the moving averages only to a certain point; if the plots do not sufficiently converge more replications are needed. The figures on the following pages show the progression of increasing the window size and the number of replications until a plot with reasonable smoothness can be selected.

The numerical value of \( w \) represents the half-width of the “window” that is used to average the output. A window size of 10 corresponds to the average of 21 observations centered on that point in the time series. Thus, each graphed point in
Welch’s Method is the calculated average of $2w + 1$ observations. As stated previously, an observation in this experiment represents a data point collected each 5 seconds of simulation time. Figure 10 begins with 10 replications and a window size of 1. The window size is increased sequentially before it no longer becomes beneficial to increase the window size. It is important to select the smallest possible window size that produces a reasonably smooth graph as a window size unnecessarily large will yield excessively large initial transient truncation points.

The following plots are from the medium size model (5th Street Corridor) for low volumes.

![Graph showing Number of Vehicles in Network vs Simulation Time (seconds)](image)

**Figure 10.** Welch’s Method for 10 Replications and a window size 1
Figure 11. Welch’s Method for 10 Replications and window size 5

Figure 12. Welch’s Method for 10 Replications and a window size 10
Figure 13. Welch’s Method for 10 Replications and a window size 15

Figure 14. Welch’s Method for 10 Replications and window size 20
Figure 15. Welch's Method for 10 Replications and window size 30

Figure 16. Welch's Method for 10 Replications and window size 40
Figure 17. Welch’s Method for 10 Replications and window size 50

Figure 18. Welch’s Method for 10 Replications and window size 75
Beyond a window size of 100, the advantages of selecting a larger window size are no longer beneficial. Thus, the plots do not appear to converge to a smooth line with the selected number of replications. Figures 19–22 demonstrate the selection of the number of replications needed to smooth the moving averages. Similarly to the selection of the window size, after a certain amount of replication there is no longer significant improvement in the smoothness of the plots. After 10 replications were examined, the number of replications was increased by 10 each time.

In this example, 40 replications were found sufficient to result in convergence of the moving averages. After 40 replications were selected, the process of determining the window size was repeated and \( w = 100 \) was selected again. The next step for Welch’s Method is to plot the initial portion of the moving averages series and visually determine
when the plot is “reasonably smooth”. By including the horizontal line representing the average value over the second half of the data, the truncation point could be selected easily.

Figure 20. Welch’s Method for 20 Replications and window size 100
Figure 21. Welch's Method for 30 Replications and window size 100

Figure 22. Welch's Method for 40 Replications and window size 100
Clearly selecting the appropriate window size is a judgment call and can vary from user to user. Each user selects the smallest possible window that can smooth (in that users’ judgment) the data. For instance, in this example a window size of 100 was selected by the author. To analyze the impact of user judgment, results were obtained for two window sizes below 100 and two above 100. Table 1 below shows the truncation points found at these different window sizes. An important trend was discovered: as the window size increases, so does the estimated truncation point. Thus, the selection of the window size has a significant impact on the location of the anticipated truncation point. It is expected that some users will tend to determine more conservative truncations points while other tend to determine short start-up periods.

<table>
<thead>
<tr>
<th>Number of Replications</th>
<th>Window Size</th>
<th>Truncation Point</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Low Volume</td>
<td>High Volume</td>
</tr>
<tr>
<td>40</td>
<td>60</td>
<td>400</td>
<td>400</td>
</tr>
<tr>
<td>40</td>
<td>80</td>
<td>500</td>
<td>450</td>
</tr>
<tr>
<td>40</td>
<td>100</td>
<td>600</td>
<td>550</td>
</tr>
<tr>
<td>40</td>
<td>120</td>
<td>700</td>
<td>650</td>
</tr>
<tr>
<td>40</td>
<td>140</td>
<td>800</td>
<td>750</td>
</tr>
</tbody>
</table>

### 4.1.2 Sensitivity to Number of Replications

Law and Kelton proposed starting with five or ten replications, based on model execution and cost [6]. In our study, ten replications were used as a starting point and the number of replications were increased until the desired smoothness is achieved. A total of 100 replications were performed, each with a different random seed. Ten replications
were randomly selected from the sample set and the average value was computed at each time step. This sampling method was repeated to obtain the averages of 20, 30, 40, and 50 replications. The entire set was used to find the average over 100 replications. The impact of using different numbers of replications for the medium model size is shown in Table 2 below.

**Table 2. Sensitivity to Number of Replications, 5th Street Model**

<table>
<thead>
<tr>
<th>Number of Replications</th>
<th>Window Size</th>
<th>Truncation Point</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Low Volume</td>
</tr>
<tr>
<td>10</td>
<td>100</td>
<td>550</td>
</tr>
<tr>
<td>20</td>
<td>100</td>
<td>550</td>
</tr>
<tr>
<td>30</td>
<td>100</td>
<td>600</td>
</tr>
<tr>
<td>40</td>
<td>100</td>
<td>600</td>
</tr>
<tr>
<td>50</td>
<td>100</td>
<td>550</td>
</tr>
<tr>
<td>100</td>
<td>100</td>
<td>600</td>
</tr>
</tbody>
</table>

As the number of replications is increased, it becomes easier to determine the truncation point as the moving average plots becomes smoother. However, the same truncation time can be read from the graph of 10 replications as that of 100 replications, shown in Table 2 for the high volume case. The trend was evident for both the small and large model sizes (results included in Appendix). This indicates that Welch’s Method can provide similar results as the number of replication is increased for this model scenario. However, it should be noted that 10 replications was used as the minimum for this experiment; it is not believed that using one, or even five replications would produce the same result as those from 100 replications.
The major factor affecting the sensitivity of the truncation point found by Welch’s Method to the number of replications used is the variability of the output data. For highly variable data, a large amount of replications may be needed to produce similar results. More analysis is needed before this conclusion can be generalized, but the fact that the results obtained from 10 and 100 replications are similar is an important finding.

4.1.3 Change in Model Size

Welch’s Method was applied to the three different model sizes: a single intersection, a small corridor, and a large grid network. The results for the Welch’s Method for each case are shown in Table 3 below. The truncation point was found using replicated averages of the number of vehicles in the network for both the low and high volume case.

<table>
<thead>
<tr>
<th>Volume</th>
<th>Truncation Point (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Small</td>
</tr>
<tr>
<td>Low</td>
<td>600</td>
</tr>
<tr>
<td>High</td>
<td>550</td>
</tr>
</tbody>
</table>

The small and medium network sizes have very similar warm-up lengths, while the warm-up period for the large network is almost three times as large. One reason the small and medium network have similar warm-up times is these two models are generally dominated by the same intersection, Spring Street and 5th Street. The small network consists of solely this intersection while the medium model contains an additional intersection to the east (West Peachtree Street) and three signalized intersections to the
west. Both Spring Street and West Peachtree Street contain five times as much volume as that on 5th Street. Thus, the time it takes to initialize the 5th Street corridor model depends primarily on the time it takes to warm-up the intersection at Spring Street. The number of vehicles in the network is the performance measure evaluated, and the intersections with higher volumes dominate the calculations. For future research, it would be beneficial to construct an experiment where the volume difference between the two cross streets is less drastic.

As expected the large model contains a longer initial transient period than the smaller models. During its steady-state conditions, the large model contains fewer than 900 vehicles in the network, while the medium and small models contain an average of 84 and 41 vehicles (respectively) for the high volume case. The main factors that determine the length of the initial transient are the distance and time a vehicle needs to travel through the network. A model with a large number of signalized intersections would be expected to reach steady-state at a later time because of delay encountered at each intersection. Similarly, if the effective green time is reduced for major movements in a network, the initial transient period would be expected to increase.

4.1.4 Welch’s Method using Travel Time

Network travel time was tested for Welch’s Method to determine if travel time is a good indicator of the performance of corridor or network. For each model size, a route was selected that is considered representative of the network and constitutes a large amount of traffic. The input volume and routing decisions were modified before the experiment was performed such that a minimum of 60 vehicles would complete the travel
time segment per hour. This number was selected based on the desire to have a sufficient amount of data to perform each method by creating an observation interval of 60 seconds.

For the first iteration of Welch’s Method, 10 replications were randomly selected and averaged. The window size was initially set at $w = 1$ for the medium network as shown in Figure 23 below.

![Figure 23. Welch's Method using Travel Time, medium model, 10 replications, w=1](image)

Next, the window size is sequentially increased until the plots become “reasonably smooth”, which could not be achieved without further replications. Using 20 replications, the window size was increased to $w = 50$ to produce the desired smoothness. The moving average plots from 20 replications are displayed in Figure 24 on the following page.
The next step of analyzing Welch’s Method is to examine the initial portion of the graph and visually select the truncation point. The first 3600 seconds of the simulation are shown in Figure 25 on the next page. From this figure, there are two different truncation points that can be selected. The first time the moving averages intersects the mean (calculated over the second half of data) is at 600 seconds and then again at 1100 seconds for the second time.
Figure 25. Initial Warm-up of Welch's Method using Travel Time, medium model, 20 replications, w = 50

An argument could be made for choosing either of these points. At 600 seconds, the model could have reached equilibrium and is experiencing a realistic spike in demand. Or, the analyst could interpret this graph as first reaching steady-state at 1100 seconds and the high values of travel time is not representative of the model. While both interpretations are valid, the author selected a truncation point of 600 seconds for this case because it is not good practice to discard data that could be representative of a realistic steady-state condition solely based on the fact that it would have a negative impact on the model performance statistics.

For the medium model size shown above, the plots generated from travel time measurements are not as smooth as those generated by using the network vehicle count. An explanation is that travel time can be a sparse measurement for small networks. For the large model, however, this is not the case. Welch’s Method for the large network is
shown below in Figure 26 as well as the warm-up period in Figure 27 on the following page.

Figure 26. Welch’s Method for Travel Time, large model, 40 replications, w = 50

For this model, 40 replications are necessary to ensure sufficient smoothness, and a window size of 50 was selected. Table 4 below shows a comparison of the truncation values obtained by Welch’s Method from the three model sizes.

**Table 4. Comparing truncations point across three models sizes**

<table>
<thead>
<tr>
<th>Number of Replications</th>
<th>Truncation Point (seconds) by model size</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Small (w = 100)</td>
</tr>
<tr>
<td>10</td>
<td>200</td>
</tr>
<tr>
<td>20</td>
<td>200</td>
</tr>
<tr>
<td>30</td>
<td>150</td>
</tr>
<tr>
<td>40</td>
<td>175</td>
</tr>
<tr>
<td>50</td>
<td>175</td>
</tr>
</tbody>
</table>
Figure 27. Welch’s Method for Travel Times, large model, 40 replications, w = 50

From Figure 27, the truncation point was determined to be at 1600 seconds. As a comparison, Table 5 below shows the truncation point found by applying the network vehicle count versus using travel time to plot the moving averages for the smaller volumes.

Table 5. Comparing Vehicle Count and Travel Time truncations points

<table>
<thead>
<tr>
<th></th>
<th>Truncation Point (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Small</td>
</tr>
<tr>
<td>Vehicle Count</td>
<td>550</td>
</tr>
<tr>
<td>Travel Time</td>
<td>175</td>
</tr>
</tbody>
</table>

From this table, it can be inferred that travel time and vehicle count both arrive at similar estimates for the length of the initial transient. However, the single intersection results varied substantially. One reason could be that measuring one movement in an
intersection (the southbound through for this case) does not represent the entire network sufficiently as the side street would have a small impact. For the medium and large networks, as long as the travel time segment chosen spans the entire network and has enough vehicles on the route, travel time can be used as a measure of equilibrium. More research is needed to determine the sufficient number of vehicles completing the route that are needed, as well as comparing the results to measurements obtained from other major routes in the network.

4.1.5 Analysis of Welch’s Method

An analysis of the issues that arose while using Welch’s Method will be discussed in Chapter 5. The benefits of using the method will be discussed, as well as a comparison of the method’s performance compared to other methods. Lastly, the criticisms and disadvantages of using Welch’s Method will be discussed with future recommendations being proposed.

4.2 Marginal Standard Error Rule (MSER)

As noted by White (1997), MSER specifies the optimal truncation point when applied to individual output sequences [13]. Thus, this method will be performed on each replication rather than performing the method on averaged output from multiple runs. In this study, 100 replications were generated for analysis of each model size and traffic demand level. The formula given in Chapter 3 is been implemented to select the local minimum value of the MSER statistic. For comparison purposes, the maximum truncation point, average truncation point, and the 95th percentile truncation point are recorded.
The selected truncation value for the MSER is the minimum value of the width of the marginal confidence interval about the truncated sample mean. A sample plot of the MSER statistic is shown in Figure 28 for the 5th Street Corridor model using a batch size of 5. The minimum value was calculated at 350 seconds for this example.

![Sample plot of the MSER-5 statistic for an individual run](image)

**Figure 28. Sample plot of the MSER-5 statistic for an individual run**

Figure 29 below shows the frequency of occurrences of the truncation values for the 5th Street model at low demand calculated by finding the minimum of the MSER-5 statistic. The Cumulative Distribution Function (CDF) for the MSER-5 case is shown below in Figure 30 on the next page for 100 replications. Similar plots for the remaining scenarios are given in Appendix C.
4.2.1 Sensitivity to Batch Size, Observation Size

The MSER-\(n\) refers to performing the procedure on the average of \(n\) batches.

White Jr. et al. (2000) noted that using a batch size of five greatly improves the results for the MSER [14]. It is recalled that in this study, a single observation consists of the
network vehicle count obtained every five seconds. Transportation models containing signalized networks can exhibit patterns when grouped in different time intervals due to the nature of traffic signals. Therefore, the MSER procedure is repeated for varying batch sizes to determine the impact batch size on the truncation value. The batch sizes tested for the five-second observation data are 1, 5, 12, and 22 batches, corresponding to simulation time windows of 5, 25, 60, and 110 seconds.

Table 6 on the next page demonstrates the sensitivity of the truncation value to the selected batch size.

### Table 6. MSER\(_n\): Number of Vehicles with different batch sizes, 5\(^{th}\) Street Model

<table>
<thead>
<tr>
<th>Simulation time covered (seconds)</th>
<th>MSER-1</th>
<th>MSER-5</th>
<th>MSER-12</th>
<th>MSER-22</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average</td>
<td>77</td>
<td>98</td>
<td>159</td>
<td>398</td>
</tr>
<tr>
<td>95(^{th}) Percentile</td>
<td>175</td>
<td>275</td>
<td>360</td>
<td>1298</td>
</tr>
</tbody>
</table>

Table 6 shows that increasing the batch size will increase the value of the truncation point. This meets intuition because as the batch size increases, the values for the earliest possible truncation points are larger and also increase more rapidly. MSER-1 and MSER-5 produce comparable truncation points while the batch sizes of 12 and 22 result in much larger truncation points.
4.2.2 Sensitivity to Observation Length

As mentioned before, an observation interval of five seconds was selected based on experience and convenience before the experiment was performed. While obtaining information for one second intervals is feasible, it can be computationally intensive. To determine the sensitivity of the determined truncation point to the observation internal, the width of the observation is changed from 5 seconds to 25, 60, and 110 seconds. The MSER-1 must be used in this set of experiments as a larger batch size would result in batch intervals that are unnecessarily large. Table 7 below shows the results of changing the observation size without using batches (MSER-1).

<table>
<thead>
<tr>
<th>Simulation time covered (seconds)</th>
<th>Optimal Truncation Time (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MSER-1</td>
</tr>
<tr>
<td>Average</td>
<td>77</td>
</tr>
<tr>
<td>95th Percentile</td>
<td>175</td>
</tr>
</tbody>
</table>

The results for increasing the interval size for the number of vehicles in the network has the same effect as increasing the batch size: increasing the interval size increases the truncation point. The results obtained from changing the observation size were almost identical to those from changing the batch size. The main reason is that the same amount of simulation time is being covered by each method. MSER-1 using 25-second batches produced the same results as MSER-5 with five-second batches. The difference between these two procedures is MSER-1 is taking one measurement at the end of the 25 seconds while MSER-5 is averaging five observations.
4.2.3 Sensitivity to Simulation Run Length

In each experiment discussed thus far the simulation run length is set to five hours to ensure the models are given sufficient time to reach “steady-state”. In this analysis the data is re-analyzed to determine the truncation points as if the model had been run for a shorter time period. That is, the later part of each run is not included in the MSER calculations. Table 8 below displays the truncation points for run lengths of 1, 2, 3, 4, and 5 hours for the MSER-5 case for the medium network size. For any run length over 2 hours, MSER-5 provides the same maximum truncation point, and very similar average truncation points. For any run length from two to five hours long, the 95\textsuperscript{th} percentile truncation points are also nearly identical.

Table 8: MSER-5: Number of Vehicles in Network for changing Run Length

<table>
<thead>
<tr>
<th>Total simulation length (seconds)</th>
<th>Optimal Truncation Time (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MSER-5</td>
</tr>
<tr>
<td>3,600</td>
<td>7,200</td>
</tr>
<tr>
<td>7,200</td>
<td>93</td>
</tr>
<tr>
<td>10,800</td>
<td>175</td>
</tr>
<tr>
<td>14,440</td>
<td></td>
</tr>
<tr>
<td>18,000</td>
<td></td>
</tr>
</tbody>
</table>

4.2.4 Change in Volume and Model Size

MSER was applied to the three selected model sizes to determine the average truncation point of each model. All four batch sizes chosen earlier were examined as well as high and low volumes for the small and medium network sizes. These values are shown in a bar graph in Figure 31 on the following page.
Table 9 on the following page shows the results for Figure 31 which consists of the average truncation point over 100 replicate runs. As anticipated, the small network has the shortest warm-up time, closely followed by the medium network, the 5th Street corridor. The results for the small and medium network were extremely close, mainly due to the similarities in the network characteristics. For these two model sizes, MSER-5 remained consistent for an increase in the volume. The large network’s average truncation point is almost 12 times larger than the medium case, which is reasonable due to the size difference.
Table 9. Average MSER-n Truncation Point for varying model and batch sizes

<table>
<thead>
<tr>
<th>Network size, volume (simulation time)</th>
<th>MSER-1 (5)</th>
<th>MSER-5 (25)</th>
<th>MSER-12 (60)</th>
<th>MSER-22 (110)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Small, Low Volume</td>
<td>60</td>
<td>71</td>
<td>115</td>
<td>365</td>
</tr>
<tr>
<td>Small, High Volume</td>
<td>64</td>
<td>74</td>
<td>133</td>
<td>261</td>
</tr>
<tr>
<td>Medium, Low Volume</td>
<td>77</td>
<td>98</td>
<td>161</td>
<td>395</td>
</tr>
<tr>
<td>Medium, High Volume</td>
<td>83</td>
<td>98</td>
<td>211</td>
<td>342</td>
</tr>
<tr>
<td>Large, Low Volume</td>
<td>1123</td>
<td>1159</td>
<td>1214</td>
<td>1238</td>
</tr>
<tr>
<td>Large, High Volume</td>
<td>1216</td>
<td>1221</td>
<td>1252</td>
<td>1527</td>
</tr>
</tbody>
</table>

In general, the higher volume scenarios have a slightly longer initial transient period than the lower volumes scenarios using MSER. This follows intuition as a model with 100 vehicles would be expected to take longer to “fill up” than a model with only ten vehicles.

4.2.5 Travel Time Comparison

As mentioned before, travel time measurements were split into observations representing individual vehicles completing the travel time segment. These observations were grouped in batches of five and the MSER-5 was performed to compare the results to those obtained from the number of vehicles in the network, shown in Table 10 below.

Table 10. Average MSER-5 Truncation Point for number of vehicles, travel time

<table>
<thead>
<tr>
<th>Network size, volume</th>
<th>Average Truncation Point (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Vehicle Count</td>
</tr>
<tr>
<td>Small, Low Volume</td>
<td>71</td>
</tr>
<tr>
<td>Small, High Volume</td>
<td>74</td>
</tr>
<tr>
<td>Medium, Low Volume</td>
<td>98</td>
</tr>
<tr>
<td>Medium, High Volume</td>
<td>98</td>
</tr>
<tr>
<td>Large, Low Volume</td>
<td>1159</td>
</tr>
<tr>
<td>Large, High Volume</td>
<td>1221</td>
</tr>
</tbody>
</table>
Based on the results from Table 10, MSER-5 does not appear to give consistent results for both travel time and number of vehicles in the system, and it is unclear why these two performance measures give such different results. MSER optimizes each data set and based on minimizing the confidence interval, thus if one performance measure is more variable than the other, the different standard deviations would affect the truncation point chosen.

4.2.6 Analysis of MSER

A full analysis of MSER will be discussed in Chapter 5. The topics that will be examined are the advantages and criticisms of the method, the ease of implementation, and the various issues encountered in this study. Recommendations will be offered on applying this method to transportation models similar to those analyzed in this study.

4.3 Volume Balancing Method

The Volume Balancing Method was the third procedure tested in this experiment. The motivation behind selecting this method is its current use of this simulation software packages. Both CORSIM and TransModeler® have an algorithm for determining when the model has reached equilibrium by comparing the percentage change in the number of vehicles in the network over a specified time interval. In this section, the sensitivity of selecting the interval over which to compare the percentage difference in volumes is analyzed.
4.3.1 Sensitivity to Interval Size

The impact of selecting the length of the time interval is tested in this experiment. CORSIM compares the number of vehicles in the network every 60 seconds as a default value; however we are interested in analyzing several values to compare the results. Our study begins with 5 second intervals, and continues with 25, 60, and 110 second intervals. The percentage difference algorithm is applied to each individual run and the average value and 95 percentile are reported in Table 11 below.

<table>
<thead>
<tr>
<th></th>
<th>VB 5s</th>
<th>VB 25s</th>
<th>VB 60s</th>
<th>VB 110s</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total simulation length (seconds)</td>
<td>5</td>
<td>25</td>
<td>60</td>
<td>110</td>
</tr>
<tr>
<td>Average</td>
<td>57</td>
<td>121</td>
<td>301</td>
<td>388</td>
</tr>
<tr>
<td>95th Percentile</td>
<td>85</td>
<td>201</td>
<td>420</td>
<td>556</td>
</tr>
</tbody>
</table>

The small interval chooses the least amount of warm-up time while the large interval selects the longest. The main reason for this is that shorter time intervals have more chances to have a two consecutive percentage change less than 12% and 8%; the first chance for the 110-second interval is at 330 seconds. There are no guidelines on selecting the interval size, and no explanation was found as to why CORSIM uses 60 seconds as a default value. The percent differences of consecutive time intervals are shown in the Figure 32-35 on the following page for the medium network size, and interval lengths of 5, 25, 60, and 110 seconds.

There are two main disadvantages of using this method to determine equilibrium. First, choosing a time interval that is too short would cause the percentage differences to be too small. Second, a network with high volume could determine a truncation point too
soon because the percentage change in volume would not fluctuate as much. At this time we cannot recommend one interval over the other and realize insufficient guidelines for determining the interval size is a disadvantage to using this method.

Figure 32. Percentage Difference in Vehicle Count, using 5-second intervals
Figure 33. Percentage Difference of Vehicle Count, using 25-second intervals

Figure 34. Percentage Difference of Vehicle Count, using 60-second intervals
Figure 35. Percentage Difference of Vehicle Count, using 100-second intervals
The goal of this research is to explore different initialization bias truncation methods for their potential implementation in transportation simulation models. The initialization bias problem has often been neglected in practice and unaccounted for it can yield inaccurate results. After a survey of literature and the techniques used by simulation models, Welch’s Method, MSER, and the Volume Balancing Method were selected for implementation and tested on three different network sizes using VISSIM®.

Throughout the process of implementing these procedures, several issues arose that will be discussed in this section. Advantages and criticisms of each method will be listed in an attempt to compare the methods. Based on the results of this experiment, recommendations for which method to use and how to set the specific parameters will be made.

5.1 Analysis of Welch’s Method

Welch’s Method is the only one of the selected methods that could not be implemented through automation and requires the most intervention from the analyst. The theory behind Welch’s Method is intuitive and the formula and methodology for plotting the moving averages is easy to calculate and implement. Welch’s Method is performed on multiple replications and therefore has the advantage of specifying the truncation point that works best for the entire set.
One advantage of using Welch’s Method is the analyst is able to visually inspect the output data to verify the model reaches steady-state. Other methods that can be automated do not require plotting the data (however such plots are highly recommended as it is critical for the analyst to observe the characteristics of the output sequence). Another advantage is that Welch’s Method can provide consistent results for different numbers of replications. Initial tests indicate that the warm-up times selected from 10 replications were almost identical to those selected from 20, 40, and 100 replications. While increasing the number of replications does result in more smoothness in the graphs, an extremely large number of replications were not needed for the VISSIM® models studied. Lastly, this method is popular and advantageous because the plots of the moving average provide a clear picture of the model reaching steady-state.

5.1.1 Issues/Criticisms of Welch’s Method

The most common criticism of graphical methods is their subjectivity due to visually selecting the truncation point. Individuals could judge the plot to be “reasonably smooth” at different locations in the time series based on their expertise and individual preferences. In addition to reading the truncation value off the graph, there are two major factors that lead to subjective results by influencing the smoothness of the plot. The first is the selection of the window size; selecting a window size that is larger than necessary will over-smooth the plots and result in a truncation point larger than needed. The rules for selecting the best window size are very flexible which can be a problem because using different window sizes leads to a range of results. Second, the selection of the scale of the y-axis for the moving averages plots determines how rough or smooth the plot
appears. There are no guidelines on how to set the range for the y-axis, however it is important to keep the scale consistent. As a rule of thumb for this study, the scale for the y-axis was determined by setting the range to twice the variation observed from the moving averages plotted with $w = 1$.

As mentioned earlier, an aid was installed to help determine when the plot reaches the mean of the moving average function. An alternative to using this method, the analyst could add a 95% confidence interval (or any other confidence band) to the mean of the second half of the data and decide steady-state has been reached once the plot falls within this region. This approach was applied to the same plot shown in Figure 3 where a warm-up time of 600 seconds was chosen. In Figure 36 below, a warm-up time of 550 seconds can be obtained using the confidence interval.

Figure 36. Confidence Interval (95%) added to Welch’s Method
Using this approach helps provide more consistent truncation values each time and should be examined for future implementation of this method.

One disadvantage evident from this experiment is that Welch’s Method has the potential to overestimate the warm-up period when using very large window sizes. A window size of 100 with five-second observations means the sliding window first begins to move through data at 500 seconds. The first point (usually close to zero when the system is started empty) is included in each calculation until the window reaches 100. This issue would effectively set a minimum truncation point to the length of the window size, which could overestimate the warm-up time needed. Lastly, the inability to automate this process could be a minor obstacle for future use of this procedure.

5.2 Analysis of MSER

The primary advantage of using MSER is that this method optimizes the truncation point by selecting the point that minimizes the width of the confidence interval about the truncated sample mean [12]. By assuming the data in the second half is more representative of steady-state conditions, and an optimum truncation point is found for each individual run. This is potentially more robust than Welch’s approach where a single truncation point is determined and applied to all replications.

Another advantage of MSER is the ability to automate the process with little intervention from the user needed. In this effort a script was made for Visual Studio .NET to compute the MSER statistic for each replication, then the minimum value and the location in the time series was found. While this method can be performed without
plotting the data series, it is highly recommended to examine the output series to verify the model is behaving correctly.

### 5.2.1 Issues/Criticisms of MSER

The biggest issue encountered with MSER is the tendency to select the truncation point at the end of the data series. The explanation for this problem is MSER can be sensitive to a data series with very similar values at the end of the simulation output data stream. This problem has been noted in literature and an attempt to mitigate this problem was suggested by Hoad et al. who proposed ignoring the last five simulation observations when determining the minimum MSER statistic [23]. In this effort the application of this rule was found to eliminate this issue in most cases, however several runs were still reaching a minimum MSER statistic towards the end of the set. Hoad et al. also suggested increasing the amount of data being collected and only considering the minimum values from the first half of the data series. This method was implemented as well (with no additional data as 5 hours should be sufficiently large). This almost completely eliminated the problem. However, there is a significant drawback to imposing this restriction on the MSER. If the method is not allowed to select a truncation point in the last half of the data, this would potentially miss the case where congestion builds in the second half of the model or if the model never reaches steady-state.

To mitigate this problem, we suggest first imposing the restriction of not selecting the truncation point in the last five observations, and then run the method again by only considering a truncation point in the first half of the data. For series having a minimum first determined near the end of the simulation output data and then near the midpoint in
the second application the individual replication should be examined to see if there is congestion in the model (due to high volume or an incident) or if MSER reported this value because observations were close together at the end of simulation output data. If the latter is the case, the value obtained in the first half of the series can be used.

Another criticism of MSER is it can be sensitive to outliers. This effect was difficult to measure because outliers in transportation models can be hard to quantify. However, this problem does exist, and Hoad et al. noted that using the average of multiple replications (five in their experiment) partially alleviated this problem [23]. The idea of using multiple replications rather than individual replications is also an issue, as Hoad et al. found that by averaging five replications, a larger percentage of the bias could be removed. This approach was not used in this experiment due to the fact that White explicitly expressed MSER “applies to individual output sequences”, but could be considered for future implementation.

The last issue with MSER is whether to use the optimal truncation point calculated for each individual series, or to use a single point for the entire set that is equal to the average value (or max, or 95%, etc. value) obtained from multiple replications. The first case ensures each replication has reached steady-state and utilized the maximum possible amount of data from each replication. However, different simulation lengths will result in truncated data sets of varying sizes, potential complicating the processing of the replication runs and their statistical analysis. Using the average value will result in a truncation point too small for the more variable cases. Alternatively, the maximum value could be used to ensure each case has reached its optimal truncation point, but this could throw away significant amounts of steady-state data in many of the replications. Lastly,
the 95th percentile truncation value could be selected to reduce the amount of unnecessarily discarded data while ensuring the majority of replications will be in steady-state.

5.3 Analysis of the Volume Balancing Method

After the Volume Balancing formula was examined closely, this method does not appear to be a good indicator of when the model has reached steady-state. The intuition behind determining equilibrium with this method is that once the network is “full”, the percent difference in the total number of vehicles in the system between observations will be relatively small for the remainder of the simulation run. However, experiments conducted for this research have found that the stability of the observations of the number of vehicles in the network is largely dependent on the chosen time interval between observations and the volume in the network. If a very small interval is chosen, the percentage difference can be small because the number of vehicles in the network at the current time is highly dependent on the number of vehicles in the network in the previous interval. For example, if the interval size is one second the observations between consecutive intervals would be expected to be highly correlated with small absolute differences. If a larger interval size is chosen, the variation in the percentage difference can be much higher. For example, in the case of the medium model size, a 60-second interval (which is the default value CORSIM uses) results in a range of percent differences of 0 to 113%, with many instances of 30% or more differences between observations seen throughout the simulation time period. Figure 34 displays these results for the medium model size using 60-second intervals. The graph of these percent
differences illustrates why this method may not be a good measure of equilibrium. Based on the Volume Balancing methodology, the point the model reaches equilibrium would occur at 900 seconds, when two consecutive points are below 12% and 8%. However, the volume continues to fluctuate for the remainder of the simulation.

When examining a network with a large volume, the graphs can look substantially different. Figure 37 below shows the percentage difference in volume for the large network. Due to the magnitude of the vehicle counts, the percentage difference in volumes becomes very small, ranging from 0% to 6.5%. Based on the results from this experiment, it is not believed this method can be relied on as a measure of equilibrium.

Figure 37. Percentage Difference of Vehicle Count for Large network, (60-second interval)
Using the Volume Balancing formula for the large network, equilibrium is obtained at 480 seconds. However, at this time the number of vehicles in the network is 632 while the model does not completely “fill” until it reaches 762 vehicles (the average number of vehicles in the network for second half of the data set). Once the network reaches a certain size, a change in volume represents a smaller percentage change. Based on the results from this experiment, it is not believed this method can be relied on as a measure of equilibrium.

5.4 Limitations

One possible limitation would be the use of the number of vehicles in the network as an equilibrium measure. If our model was given a demand greater than capacity, the traffic signals would effectively meter the incoming vehicles and only a certain number of vehicles will be let in the system, no matter how high the demand. Also, if a network has a large volume, looking at the network vehicle count may not be able to account for a single intersection that fails and begins to form a small queue. Thus, it is important to be cautious if using only volume as a measure of equilibrium.

Travel time could be used to capture characteristics of the network that the vehicle count would not account for, such as a failed traffic signal. However, it has the disadvantage of only analyzing the consistency of the particular route being considered, as it would be extremely tedious to apply the methodology to every route in the network. Another limitation of using travel time to detect the initial transient is it can be a sparse measurement. A route that spans the entire network is desired, however, longer routes
could have a higher percentage of vehicles turning off of the mainline, resulting in fewer vehicles that complete the travel time segment from start to finish.

5.5 Conclusion

All three methods presented in this study provide comparable results for the truncation point of the steady-state mean. As the true value of the steady-state mean is unknown, we are unable to measure the amount of bias removed from the results and at what time in the sequence the correct truncation point occurs. However, the results from implementing these procedures indicate that Welch’s Method provides the most consistent results and would be the most desirable to use in practice.

The most appealing characteristic of Welch’s Method is the ability to provide extremely consistent results for an increasing the number of replications; consistent truncation points can be obtained from 10 to 100 replications. The same result was not found for MSER and Volume Balancing methods. Another important aspect of Welch’s Method is its ability to determine the same length of the initial transient by using both vehicle counts and travel times. This was not true for MSER and the Volume Balancing Method is limited to only looking at the network vehicle count.

It is also important to have the analyst involved in the decision so that they are not completely removed from the process. MSER has the potential to be a useful tool, but additional efforts are needed to better guide its use in transportation applications. To improve the application of Welch’s Method, the addition of a confidence band for the second half of the data is suggested.
APPENDIX A: DEVELOPMENT OF VISSIM® MODEL

A main goal of this study was to perform the warm-up procedures on three distinctly different models sizes. However, we wanted the larger models to build upon a small model so that we could have a similar area to compare at each level. This was accomplished by first building the large network and inputting the routing decisions and signal timing information. Kate D’Ambrosio, a graduate research student at Georgia Tech, created the VISSIM® model of the Georgia Tech campus and surround area used in this study. This was an extensive process and took several months of labor to code the massive network. The default values for the routing decision used for this study were for 80% of the vehicles to continue through, 15% turn right, and 5% turn left. 27 vehicle input were inserted into the network at all boundary points.

The 87 signalized intersections were set up with a Ring Barrier Controller (RBC) in VISSIM® with a default value of 60 seconds for the cycle length. Traffic count information was obtained for the 5th Street corridor and the routing decisions were updated to reflect actual movements. Signal timing for the corridor was obtained and the RBC controllers were adjusted accordingly. For the corridor, Spring Street and West Peachtree both used 110 second cycle lengths, while 5th and Fowler, and 5th and Techwood Drive used 75 seconds. As the majority of the analysis was performed on this corridor, it was important to ensure it was as realistic as possible.

After the parameters had been updated for the large Georgia Tech network, the model was reduced in size to include 5th Street from Dalney Street to West Peachtree Street. This model was carved out of the larger network to ensure the signal timing and
routing decisions were consistent across all three model sizes. To create the single intersection case, the model was further reduced to 5th Street and Spring Street.

Figure 38. The three Model Sizes and relative location within the large model
Vehicle Input Tables

Table 12. 5th Street at Spring Street Vehicle Inputs

<table>
<thead>
<tr>
<th>Link Name</th>
<th>Number of Vehicles/Hour (per volume level)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Medium</td>
</tr>
<tr>
<td>EB 5th Street</td>
<td>200</td>
</tr>
<tr>
<td>WB 5th Street</td>
<td>200</td>
</tr>
<tr>
<td>SB Spring Street</td>
<td>1000</td>
</tr>
</tbody>
</table>

Table 13. 5th Street Corridor Vehicle Inputs

<table>
<thead>
<tr>
<th>Link Name</th>
<th>Number of Vehicles/Hour (per volume level)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Medium</td>
</tr>
<tr>
<td>EB 5th Street</td>
<td>200</td>
</tr>
<tr>
<td>WB 5th Street</td>
<td>100</td>
</tr>
<tr>
<td>SB State Street</td>
<td>100</td>
</tr>
<tr>
<td>SB Fowler Street</td>
<td>100</td>
</tr>
<tr>
<td>NB Fowler Street</td>
<td>100</td>
</tr>
<tr>
<td>SB Techwood Drive</td>
<td>100</td>
</tr>
<tr>
<td>NB Techwood Drive</td>
<td>100</td>
</tr>
<tr>
<td>Spring Street</td>
<td>1000</td>
</tr>
<tr>
<td>West Peachtree Street</td>
<td>1000</td>
</tr>
</tbody>
</table>
Table 14. 5th Street Corridor Vehicle Inputs

<table>
<thead>
<tr>
<th>Link Name</th>
<th>Number of Vehicles/Hour (per volume level)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Medium</td>
</tr>
<tr>
<td>Ferst Dr. EB</td>
<td>100</td>
</tr>
<tr>
<td>Techwood Dr NB</td>
<td>100</td>
</tr>
<tr>
<td>5th Street WB</td>
<td>250</td>
</tr>
<tr>
<td>Peachtree St SB</td>
<td>500</td>
</tr>
<tr>
<td>Spring St SB</td>
<td>1500</td>
</tr>
<tr>
<td>W. Peachtree St NB</td>
<td>1500</td>
</tr>
<tr>
<td>7th Street WB</td>
<td>100</td>
</tr>
<tr>
<td>Cyprus St SB</td>
<td>100</td>
</tr>
<tr>
<td>Northside Dr NB</td>
<td>600</td>
</tr>
<tr>
<td>North Ave EB</td>
<td>300</td>
</tr>
<tr>
<td>Tech Way WB</td>
<td>100</td>
</tr>
<tr>
<td>Strong Street NB</td>
<td>100</td>
</tr>
<tr>
<td>Donald Lee Holdwell Pkwy WB</td>
<td>200</td>
</tr>
<tr>
<td>West Marietta St SB</td>
<td>400</td>
</tr>
<tr>
<td>Dillian St SB</td>
<td>100</td>
</tr>
<tr>
<td>Holly Street SB</td>
<td>100</td>
</tr>
<tr>
<td>Ikea Exit SB</td>
<td>100</td>
</tr>
<tr>
<td>Northside Dr SB</td>
<td>600</td>
</tr>
<tr>
<td>Howell Mill SB</td>
<td>300</td>
</tr>
<tr>
<td>Huff Rd EB</td>
<td>100</td>
</tr>
<tr>
<td>Ethel St EB</td>
<td>100</td>
</tr>
<tr>
<td>Peachtree St NB</td>
<td>500</td>
</tr>
<tr>
<td>Ponce De Leon WB</td>
<td>400</td>
</tr>
<tr>
<td>4th Street WB</td>
<td>200</td>
</tr>
<tr>
<td>10th Street WB</td>
<td>120</td>
</tr>
<tr>
<td>Travel Time probe vehicle</td>
<td>100</td>
</tr>
</tbody>
</table>
APPENDIX B: ADDITIONAL PLOTS FOR WELCH’S METHOD

Figure 39. Welch's method for small network, 40 replications, w = 100

Figure 40. Welch's Method for Identification of warm-up,
Small network, 40 replications, w = 100
Figure 41. Welch's Method for large network, 50 replications, w = 150

Figure 42. Welch's Method for Identification of warm-up, Large network, 50 replications, w = 150
APPENDIX C: MSER GRAPHS

The following section presents the graphs from the MSER truncation method. The Frequency of Occurrences and Cumulative Distribution Function (CDF) are displayed for each model size. First the CDF and Frequency plot are shown for the small network size using MSER-5, followed by the CDF and Frequency plot for the large network using MSER-5. Figure 29 and Figure 30 showed the results of MSER-5 for the medium network.
Figure 43. Cumulative Distribution Function: MSER-5, small model, low volume

Figure 44. Frequency of Occurrences: MSER-5, small model size, low volume
Figure 45. Cumulative Distribution Function: MSER-5, large model, low volume

Figure 46. Frequency of Occurrences: MSER-5, small model size, low volume
APPENDIX D: VISUAL BASIC™ CODE

Two sets of Visual Basic™ scripts, written by Georgia Tech researcher Wonho Suh are included. After the data collection points were set up in VISISM®, a script was created to extract the desired information from VISSIM®. There was one script written for each network size, with the ability to adjust the input volume. Next, a script was written to perform the calculations for MSER and Volume Balancing Method. Welch’s Method differs because it requires plotting incremental window sizes and observing the smoothness of the plots. This procedure was performed in a separate spreadsheet designed to generate the plots.
Visual Basic™ Script to collect statistics from VISSIM® medium network size

Imports System.Text
Imports VISSIM_COMSERVERLib
Imports System.Runtime.InteropServices
Imports Microsoft.Office.Interop
Imports System.Convert
Imports System.Math
Imports System.IO

Public Class Warmup
    Delegate Sub VB_Reflect(ByVal a As Integer, ByVal b As String, ByVal c As Integer)

    Dim objApp As Excel.Application
    Dim objbook As Excel._Workbook
    Dim objBooks As Excel.Workbooks
    Dim objSheets As Excel.Sheets
    Dim objSheet1 As Excel._Worksheet
    Dim objSheet2 As Excel._Worksheet
    Dim objSheet3 As Excel._Worksheet

    Dim Vissim As Vissim
    Dim Simulation As Simulation
    Dim Net As Net
    Dim Vehicles As Vehicles
    Dim Vehicle As Vehicle
    Dim Links As Links
    Dim Link As Link
    Dim Eval As Evaluation
    Dim LinkEval As LinkEvaluation

    Dim TTimes As TravelTimes
    Dim TTime(0 To 50) As TravelTime
    Dim Delays As Delays
    Dim Delay(0 To 50) As Delay

    Dim Detectors As DataCollections
    Dim Detec(0 To 50) As DataCollection
    Dim Detector As DataCollectionEvaluation

    Dim DataCollections As DataCollections
    Dim DataCollection As DataCollectionEvaluation

    Dim VissimRandom As Integer
    Dim RunCount As Integer
    Dim x As Integer
    Dim xx As Integer
    Dim xxx As Integer
    Dim xxxx As Integer
    Dim SimTime As Long

    Dim Start As Date
Dim Start2 As Date

Private Sub Form1_Load(ByVal sender As System.Object, ByVal e As System.EventArgs) Handles MyBase.Load
    Console.WriteLine(Now())
    Start = Now()
    Start2 = Now()
    Randomize()
    objApp = New Excel.Application
    objBooks = objApp.Workbooks
    objbook = objBooks.Add
    objSheets = objbook.Worksheets
    objSheet1 = objSheets(1)
    objApp.Visible = True

    While RunCount < 100 ' Total Number of Runs
        RunCount = RunCount + 1
        VissimRandom = Int(Rnd() * 1000)
        Vissim = CreateObject("vissim.vissim")
        Simulation = Vissim.Simulation
        Vissim.LoadNet("C:\Tmp3\vissim\5th st luke.inp")

        objSheet1.Cells(1 + 4000 * (RunCount - 1), 1) = "Run NO"
        objSheet1.Cells(1 + 4000 * (RunCount - 1), 3) = "VISSIM seed"
        objSheet1.Cells(1 + 4000 * (RunCount - 1), 5) = "Spring Vol"
        objSheet1.Cells(1 + 4000 * (RunCount - 1), 7) = "5th Vol"

        Dim i As Integer
        For i = 0 To 6
            objSheet1.Cells(2 + 4000 * (RunCount - 1), 2 + 26 * i) = "Time"
        Next

        objSheet1.Cells(2 + 4000 * (RunCount - 1), 3) = "In system"
        objSheet1.Cells(2 + 4000 * (RunCount - 1), 55) = "SB T Ttime"
        objSheet1.Cells(2 + 4000 * (RunCount - 1), 56) = "NO VEH"
        objSheet1.Cells(2 + 4000 * (RunCount - 1), 57) = "Total"

        objSheet1.Cells(2 + 4000 * (RunCount - 1), 81) = "EB1 Ttime"
        objSheet1.Cells(2 + 4000 * (RunCount - 1), 82) = "NO VEH"
        objSheet1.Cells(2 + 4000 * (RunCount - 1), 83) = "Total"

        objSheet1.Cells(2 + 4000 * (RunCount - 1), 107) = "EB2 Ttime"
        objSheet1.Cells(2 + 4000 * (RunCount - 1), 108) = "NO VEH"
        objSheet1.Cells(2 + 4000 * (RunCount - 1), 109) = "Total"

        objSheet1.Cells(2 + 4000 * (RunCount - 1), 133) = "WB1 Ttime"
Run()
Console.WriteLine(Abs(DateDiff(DateInterval.Second, Start2, Now())) & " sec " & RunCount)
Start2 = Now()
End While

Console.WriteLine(Abs(DateDiff(DateInterval.Second, Start, Now())) & " " & RunCount)

End Sub

Sub Run()
Vissim.LoadLayout("c:\tmp3\vissim\lukemedium.ini")
Vissim.ShowMinimized()
Vissim.Graphics.AttValue("visualization") = 0

Net = Vissim.Net
Vehicles = Vissim.Net.Vehicles
Links = Net.Links
Simulation.Period = 999999999999
Simulation.RandomSeed = VissimRandom
Simulation.Resolution = 1

Eval = Vissim.Evaluation
Eval.AttValue("delay") = True
Eval.AttValue("datacollection") = True
Eval.AttValue("vehiclerecord") = True
Eval.AttValue("traveltime") = True

TTimes = Vissim.Net.TravelTimes
Delays = Vissim.Net.Delays
Detector = Vissim.Evaluation.DataCollectionEvaluation
Detector.LoadConfiguration("c:\tmp2\gt.qmk")
Detectors = Vissim.Net.DataCollections

Dim controllers As SignalControllers
Dim controller As SignalController
controllers = Vissim.Net.SignalControllers

Dim groups As SignalGroups
Dim group As SignalGroup

For x = 1 To controllers.Count
    controller = controllers(x)
    groups = Vissim.Net.SignalControllers(x).SignalGroups
Next

Dim Inputs As VehicleInputs
Inputs = Vissim.Net.VehicleInputs

For x = 1 To Inputs.Count  ' Change input volume here
  If Inputs(x).Name = "SB" Then
    Inputs(x).AttValue("volume") = 1000
  ElseIf Inputs(x).Name = "EB" Then
    Inputs(x).AttValue("volume") = 200
  ElseIf Inputs(x).Name = "NB" Then
    Inputs(x).AttValue("volume") = 200
  End If
Next x

objSheet1.Cells(1 + (RunCount - 1) * 4000, 2) = RunCount
objSheet1.Cells(1 + (RunCount - 1) * 4000, 4) = Simulation.RandomSeed
objSheet1.Cells(1 + (RunCount - 1) * 4000, 6) = ""
objSheet1.Cells(1 + (RunCount - 1) * 4000, 8) = ""

For xx = 1 To TTimes.Count
  If TTimes(xx).Name = "1" Then
    TTime(1) = TTimes(xx)
  End If
Next

While 1 > 0
  Simulation.RunSingleStep()
  SimTime = Simulation.AttValue("elapsedtime")

  If SimTime = 18001 Then
    Simulation.Stop()
    Vissim.Exit()
    Exit While
  End If

  Dim tempcount As Integer
  Dim ii As Integer

  xxx = 1
  If (SimTime - xxx) Mod 5 = 0 And SimTime > 1 Then
    For ii = 0 To 6
      objSheet1.Cells((SimTime - xxx) / 5 + 2 + (RunCount - 1) * 4000, 1 + ii * 26) = Int((SimTime - xxx) / 5)
      objSheet1.Cells((SimTime - xxx) / 5 + 2 + (RunCount - 1) * 4000, 2 + ii * 26) = SimTime - xxx
    Next

    objSheet1.Cells((SimTime - xxx) / 5 + 2 + (RunCount - 1) * 4000, 3) = Vehicles.Count
    objSheet1.Cells((SimTime - xxx) / 5 + 2 + (RunCount - 1) * 4000, 55) = TTime(1).GetResult(SimTime - 1, "traveltime", "", 0)
    objSheet1.Cells((SimTime - xxx) / 5 + 2 + (RunCount - 1) * 4000, 56) = TTime(1).GetResult(SimTime - 1, "nvehicles", "", 0)
    objSheet1.Cells((SimTime - xxx) / 5 + 2 + (RunCount - 1) * 4000, 57) = TTime(1).GetResult(SimTime - 1, "traveltime", "", 0) * TTime(1).GetResult(SimTime - 1, "nvehicles", "", 0)
End If
End While
End Sub
End Class
VB Script to perform MSER and Volume Balancing Method on vehicle count and travel time for medium model size

Imports System.Text
Imports System.Runtime.InteropServices
Imports Microsoft.Office.Interop
Imports System.Convert
Imports System.Math
Imports System
Imports System.IO

Public Class Warmup
    Delegate Sub VB_Reflect(ByVal a As Integer, ByVal b As String, ByVal c As Integer)

    Dim objApp As Excel.Application
    Dim objbook As Excel._Workbook
    Dim objBooks As Excel.Workbooks
    Dim objSheets As Excel.Sheets
    Dim objSheet1 As Excel._Worksheet

    Dim objApp2 As Excel.Application
    Dim objbook2 As Excel._Workbook
    Dim objBooks2 As Excel.Workbooks
    Dim objSheets2 As Excel.Sheets
    Dim objSheet2 As Excel._Worksheet

    Dim Start As Date
    Dim Start2 As Date

    Private Sub Form1_Load(ByVal sender As System.Object, ByVal e As System.EventArgs) Handles MyBase.Load
        Console.WriteLine(Now())
        Start = Now()
        Start2 = Now()

        objApp = New Excel.Application
        objBooks = objApp.Workbooks
        objbook = objBooks.Add

        objSheets = objbook.Worksheets
        objSheet1 = objSheets(1)
        objApp.Visible = True

        objApp2 = New Excel.Application
        objbook2 = objApp2.Workbooks.Open("C:\tmp3\output\medium_original.xlsx")
        objApp2.Visible = False
        objSheet2 = objbook2.Worksheets("sheet1")

        Dim RunNo As Integer
        Dim Interval As Integer
        Dim b As Integer
        Dim i As Integer
        Dim ii As Integer

        98
Dim iii As Integer
Dim Cutoff(0 To 5)

Cutoff(1) = 1800 ' x5 = 9000s
Cutoff(2) = 360 ' x25 = 9000s
Cutoff(3) = 150 ' x60 = 9000s
Cutoff(4) = 82 ' x110 = 9020s

For i = 0 To 19
    objSheet1.Cells(1, 1 + i * 10).value = "Run NO"
Next

objSheet1.Cells(1, 2).value = "VC M1 5s"
objSheet1.Cells(1, 3).value = "VC M5 25s"
objSheet1.Cells(1, 4).value = "VC M12 60s"
objSheet1.Cells(1, 5).value = "VC M22 110s"

objSheet1.Cells(1, 22).value = "VC M1 5s"
objSheet1.Cells(1, 23).value = "VC M1 25s"
objSheet1.Cells(1, 24).value = "VC M1 60s"
objSheet1.Cells(1, 25).value = "VC M1 110s"

objSheet1.Cells(1, 42).value = "VC M5 1hr"
objSheet1.Cells(1, 43).value = "VC M5 2hr"
objSheet1.Cells(1, 44).value = "VC M5 3hr"
objSheet1.Cells(1, 45).value = "VC M5 4hr"
objSheet1.Cells(1, 46).value = "VC M5 5hr"

objSheet1.Cells(1, 62).value = "VB 5s"
objSheet1.Cells(1, 63).value = "VB 25s"
objSheet1.Cells(1, 64).value = "VB 60s"
objSheet1.Cells(1, 65).value = "VB 110s"
objSheet1.Cells(1, 66).value = "5s NO"
objSheet1.Cells(1, 67).value = "25s NO"
objSheet1.Cells(1, 68).value = "60s NO"
objSheet1.Cells(1, 69).value = "110s NO"

objSheet1.Cells(1, 102).value = "TT M1"
objSheet1.Cells(1, 103).value = "TT M5"
objSheet1.Cells(1, 104).value = "TT M10"
objSheet1.Cells(1, 105).value = "TT M20"

objSheet1.Cells(1, 112).value = "TT M5 1hr"
objSheet1.Cells(1, 113).value = "TT M5 2hr"
objSheet1.Cells(1, 114).value = "TT M5 3hr"
objSheet1.Cells(1, 115).value = "TT M5 4hr"
objSheet1.Cells(1, 116).value = "TT M5 5hr"

Dim Count(0 To 0, 0 To 100, 0 To 5, 0 To 4000)
Dim TTime(0 To 5, 0 To 100, 0 To 5, 0 To 10000)
Dim TTimeWhen(0 To 5, 0 To 100, 0 To 5, 0 To 10000)

For RunNo = 1 To 52
    Dim TempCount(0 To 10)
    ReDim TempCount(0 To 10)
Console.WriteLine(RunNo & " start " & Now())

For i = 0 To 19
    objSheet1.Cells(1 + (RunNo), 1 + i * 10).value = RunNo
Next

' read from excel
For i = 1 To 3599
    Count(0, RunNo, 1, i) = objSheet2.Cells(2 + i + (RunNo - 1) * 4000, 3).value
Next

    For ii = 1 To 1
        ' total route number
        If objSheet2.Cells(2 + i + (RunNo - 1) * 4000, 30 + 26 * ii).value > 0 Then
            For iii = 1 To objSheet2.Cells(2 + i + (RunNo - 1) * 4000, 56).value
                TempCount(ii) = TempCount(ii) + 1
                TTime(ii, RunNo, 1, TempCount(ii)) = objSheet2.Cells(2 + i + (RunNo - 1) * 4000, 55).value
                TTimeWhen(ii, RunNo, 1, TempCount(ii)) = i * 5
            Next
        End If
    Next
Next

Dim IntCount(0 To 10)
IntCount(1) = 1
IntCount(2) = 5
IntCount(3) = 12
IntCount(4) = 22

Dim Temp0 As Integer

For Temp0 = 2 To 4
    Interval = IntCount(Temp0)
    For i = 1 To Int(3599 / Interval)
        Dim Temp1 As Single = 0
        Dim Temp2 As Single = 0
        For iii = 1 To Interval
            Temp1 = Temp1 + Count(0, RunNo, 1, (i - 1) * Interval + iii)
        Next
        Count(0, RunNo, Temp0, i) = Temp1 / Interval
    Next
Next
objSheet1.Cells(RunNo + 1, 7) = Count(0, RunNo, 1, 3599)

Dim IntTT(0 To 10)
IntTT(1) = 1
IntTT(2) = 5
IntTT(3) = 10
IntTT(4) = 20

For Temp0 = 2 To 4
    Interval = IntTT(Temp0)
    For ii = 1 To 1
        For i = 1 To IntCount(Temp0)
            Dim Temp3 As Single = 0
            For iii = 1 To Interval
                Temp3 = Temp3 + TTime(iii, RunNo, 1, (i - 1) * Interval + iii)
            Next
            TTime(ii, RunNo, Temp0, i) = Temp3 / Interval
            TTimeWhen(ii, RunNo, Temp0, i) = TTimeWhen(ii, RunNo, 1, i * Interval)
        Next
    Next
Next

For Temp0 = 1 To 4
    Interval = IntCount(Temp0)
    Dim CountTerm1(0 To Int(3599 / Interval)) As Single
    Dim CountTerm2(0 To Int(3599 / Interval)) As Single
    ReDim CountTerm1(0 To Int(3599 / Interval))
    ReDim CountTerm2(0 To Int(3599 / Interval))
    For i = 0 To Int(3599 / Interval) - 1
        Dim Temp4 As Single = 0
        Dim Temp5 As Single = 0
        Dim Temp6 As Single = 0
        Dim Temp7 As Single = 0
        Dim Temp8 As Single = 0
        For ii = 1 To Int(3599 / Interval) - 1 - i + 1
            Temp4 = Temp4 + Count(0, RunNo, Temp0, i + ii) / Temp6 + 1
        Next
        CountTerm1(i) = Temp4 / Temp6
        For iii = i + 1 To Int(3599 / Interval)
            Temp7 = Temp7 + (Count(0, RunNo, Temp0, iii) - CountTerm1(i)) * (Count(0, RunNo, Temp0, iii) - CountTerm1(i))
        Next
        CountTerm2(i) = Temp7 / (Int(3599 / Interval) - i) / (Int(3599 / Interval) - i)
Next

Dim Temp9 As Single = CountTerm2(1)
Dim Temp10 As Single = Interval * 5

For i = 1 To Int(3599 / Interval) - 1 - Cutoff(Temp0)
    If CountTerm2(i) < Temp9 Then
        Temp9 = CountTerm2(i)
        Temp10 = i * Interval * 5
    End If
Next
objSheet1.Cells(RunNo + 1, Temp0 + 1) = Temp10
Next

For Temp0 = 1 To 4
    Interval = IntCount(Temp0)
    Dim CountTerm1(0 To Int(3599 / Interval)) As Single
    Dim CountTerm2(0 To Int(3599 / Interval)) As Single

    ReDim CountTerm1(0 To Int(3599 / Interval))
    ReDim CountTerm2(0 To Int(3599 / Interval))

    For i = 0 To Int(3599 / Interval) - 1 ' 0 <= d < n
        Dim Temp4 As Single = 0
        Dim Temp5 As Single = 0
        Dim Temp6 As Single = 0
        Dim Temp7 As Single = 0
        Dim Temp8 As Single = 0

        For ii = 1 To Int(3599 / Interval) - 1 - i + 1
            Temp4 = Temp4 + Count(0, RunNo, 1, i * Interval + ii * Interval)
        Next
        Temp6 = Temp6 + 1
    Next
    CountTerm1(i) = Temp4 / Temp6

    For iii = i + 1 To Int(3599 / Interval)
        Temp7 = Temp7 + (Count(0, RunNo, Temp0, iii) - CountTerm1(i)) * (Count(0, RunNo, Temp0, iii) - CountTerm1(i))
    Next
    CountTerm2(i) = Temp7 / (Int(3599 / Interval) - i) / (Int(3599 / Interval) - i)
    Next

Dim Temp9 As Single = CountTerm2(1)
Dim Temp10 As Single = Interval * 5
Dim Temp12 As Single = Interval * 5

For i = 1 To Int(3599 / Interval) - 1 - Cutoff(Temp0)
    If CountTerm2(i) < Temp9 Then
        Temp9 = CountTerm2(i)
        Temp10 = i * Interval * 5
    End If

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Next
objSheet1.Cells(RunNo + 1, Temp0 + 21) = Temp10
Next

Dim RunLength(0 To 10)
RunLength(1) = 144 '144 x 25 = 3600s or 1hr
RunLength(2) = 288 '288 x 25 = 7200s or 2hr
RunLength(3) = 432 '432 x 25 = 10800s or 3hr
RunLength(4) = 576 '576 x 25 = 14400s or 4hr
RunLength(5) = 720 '720 x 25 = 18000s or 5hr

For Temp0 = 1 To 5
    Dim Length As Integer
    Length = RunLength(Temp0)

    Dim CountTerm1(0 To Length) As Single
    Dim CountTerm2(0 To Length) As Single

    ReDim CountTerm1(0 To Length)
    ReDim CountTerm2(0 To Length)

    For i = 0 To Length - 1
        Dim Temp4 As Single = 0
        Dim Temp5 As Single = 0
        Dim Temp6 As Single = 0
        Dim Temp7 As Single = 0
        Dim Temp8 As Single = 0

        For ii = 1 To Length - 1 - i + 1
            Temp4 = Temp4 + Count(0, RunNo, 2, i + ii)
            Temp6 = Temp6 + 1
        Next

        CountTerm1(i) = Temp4 / Temp6

        For iii = i + 1 To Length
            Temp7 = Temp7 + (Count(0, RunNo, 2, iii) - CountTerm1(i)) * (Count(0, RunNo, 2, iii) - CountTerm1(i))
        Next

        CountTerm2(i) = Temp7 / (Length - i) / (Length - i)
    Next

    Dim Temp9 As Single = CountTerm2(1)
    Dim Temp10 As Single = 25

    For i = 1 To Length - 1 - Cutoff(2)
        If CountTerm2(i) < Temp9 Then
            Temp9 = CountTerm2(i)
            Temp10 = i * 25
        End If
Next
objSheet1.Cells(RunNo + 1, Temp0 + 41) = Temp10
Next

'Volume Balancing with different interval
For Temp0 = 1 To 4
    Interval = IntCount(Temp0)
    Dim Temp4 As Single = 0
    Dim Temp5 As Single = 0
    Dim Temp6 As Single = 0
    Dim Temp7 As Integer = 0

    For i = 3 To Int(3599 / Interval) - 1
        Temp4 = Count(0, RunNo, 1, Interval * (i - 2))
        Temp5 = Count(0, RunNo, 1, Interval * (i - 1))
        Temp6 = Count(0, RunNo, 1, Interval * (i - 0))

        If (Abs(Temp4 - Temp5) / Temp4) < 0.12 And (Abs(Temp5 - Temp6) / Temp5) < 0.08 Then
            Temp7 = Temp7 + 1
            If Temp7 = 1 Then
                objSheet1.Cells(RunNo + 1, Temp0 + 61) = i

        End If
    Next
Next

'Travel Time MSER with different batch sizes
For Temp0 = 1 To 4
    Interval = IntTT(Temp0)
    Dim TTTerm1(0 To Int(TempCount(1) / Interval)) As Single
    Dim TTTerm2(0 To Int(TempCount(1) / Interval)) As Single

    ReDim TTTerm1(0 To Int(TempCount(1) / Interval))
    ReDim TTTerm2(0 To Int(TempCount(1) / Interval))

    For i = 0 To Int(TempCount(1) / Interval) - 1 ' 0 <= d < n
        Dim Temp4 As Single = 0
        Dim Temp5 As Single = 0
        Dim Temp6 As Single = 0
        Dim Temp7 As Single = 0
        Dim Temp8 As Single = 0

        For ii = 1 To Int(TempCount(1) / Interval) - 1 + i
            Temp4 = Temp4 + TTime(1, RunNo, Temp0, i + ii)
            Temp6 = Temp6 + 1
        Next

        TTTerm1(i) = Temp4 / Temp6
For iii = i + 1 To Int(TempCount(1) / Interval) 
    Temp7 = Temp7 + (TTime(1, RunNo, Temp0, iii) - TTTerm1(i)) * (TTime(1, RunNo, Temp0, iii) - TTTerm1(i)) 
Next 

TTTerm2(i) = Temp7 / (Int(TempCount(1) / Interval) - i) / (Int(TempCount(1) / Interval) - i) 
Next 

'Find the minimum value 
Dim Temp9 As Single = TTTerm2(1) 
Dim Temp10 As Single = TTimeWhen(1, RunNo, Temp0, 1) 
For i = 1 To Int(TempCount(1) / Interval) - 1 - Cutoff(Temp0) 
    If TTTerm2(i) < Temp9 Then 
        Temp9 = TTTerm2(i) 
        Temp10 = TTimeWhen(1, RunNo, Temp0, i) 
    End If 
Next 
objSheet1.Cells(RunNo + 1, Temp0 + 101) = Temp10 
Next 

'Travel Time MSER5 with different run lengths 
For i = 1 To Int(TempCount(1) / 5) 
    If TTimeWhen(1, RunNo, 2, i) <= 3600 Then 
        RunLength(1) = i 
    ElseIf TTimeWhen(1, RunNo, 2, i) <= 7200 Then 
        RunLength(2) = i 
    ElseIf TTimeWhen(1, RunNo, 2, i) <= 10800 Then 
        RunLength(3) = i 
    ElseIf TTimeWhen(1, RunNo, 2, i) <= 14400 Then 
        RunLength(4) = i 
    End If 
    RunLength(5) = Int(TempCount(1) / 5) 
Next 

For Temp0 = 1 To 5 
    Dim Length As Integer 
    Length = RunLength(Temp0) 
    Dim TTimeTerm1(0 To Length) As Single 
    Dim TTimeTerm2(0 To Length) As Single 
    ReDim TTimeTerm1(0 To Length) 
    ReDim TTimeTerm2(0 To Length) 
    For i = 0 To Length - 1 
        Dim Temp4 As Single = 0 
        Dim Temp5 As Single = 0 
        Dim Temp6 As Single = 0 
        Dim Temp7 As Single = 0 
        Dim Temp8 As Single = 0 
        For ii = 1 To Length - 1 - i + 1 
            Temp4 = Temp4 + TTime(1, RunNo, 2, i + ii) 
        Next 
    Next 

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Temp6 = Temp6 + 1
Next

TTimeTerm1(i) = Temp4 / Temp6

For iii = i + 1 To Length
Temp7 = Temp7 + (TTime(1, RunNo, 2, iii) - TTimeTerm1(i)) * (TTime(1, RunNo, 2, iii) - TTimeTerm1(i))
Next

TTimeTerm2(i) = Temp7 / (Length - i) / (Length - i)
Next

'Finding the minimum value
Dim Temp9 As Single = TTimeTerm2(1)
Dim Temp10 As Single = TTimeWhen(1, RunNo, 2, 1)

For i = 1 To Length - 1 - Cutoff(2)
    If TTimeTerm2(i) < Temp9 Then
        Temp9 = TTimeTerm2(i)
        Temp10 = TTimeWhen(1, RunNo, 2, i)
    End If
Next
objSheet1.Cells(RunNo + 1, Temp0 + 111) = Temp10
Next
Next

Console.WriteLine(Abs(DateDiff(DateInterval.Second, Start, Now()))) & "      ")
End Sub
End Class
REFERENCES


